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Total marks — 140

Attempt ALL questions.

Reference may be made to the Physics Relationships Sheet X757/77/11 and the Data Sheet on *Page 02*.

Write your answers clearly in the spaces provided in this booklet. Additional space for answers and rough work is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting. Any rough work must be written in this booklet. You should score through your rough work when you have written your final copy.

Care should be taken to give an appropriate number of significant figures in the final answers to calculations.

Use blue or black ink.

Before leaving the examination room you must give this booklet to the Invigilator; if you do not, you may lose all the marks for this paper.





DATA SHEET

COMMON PHYSICAL QUANTITIES

Quantity	Symbol	Value	Quantity	Symbol	Value
Gravitational					
acceleration on Earth	g	9⋅8 m s ⁻²	Mass of electron	m _e	9·11 × 10 ^{−31} kg
Radius of Earth	R _E	6·4 × 10 ⁶ m	Charge on electron	e	-1.60×10^{-19} C
Mass of Earth	$M_{\rm E}$	6∙0 × 10 ²⁴ kg	Mass of neutron	m _n	1⋅675 × 10 ⁻²⁷ kg
Mass of Moon	M _M	7.3×10^{22} kg	Mass of proton	m _p	1⋅673 × 10 ⁻²⁷ kg
Radius of Moon	R _M	1.7 × 10 ⁶ m	Mass of alpha particle	m_{α}	6∙645 × 10 ⁻²⁷ kg
Mean Radius of			Charge on alpha		
Moon Orbit		3∙84 × 10 ⁸ m	particle		3·20 × 10 ^{−19} C
Solar radius		6∙955 × 10 ⁸ m	Planck's constant	h	6∙63 × 10 ^{−34} J s
Mass of Sun		2·0 × 10 ³⁰ kg	Permittivity of free		
1 AU		1∙5 × 10 ¹¹ m	space	ε_0	$8.85 \times 10^{-12} \mathrm{Fm}^{-1}$
Stefan-Boltzmann			Permeability of free		
constant	σ	$5.67 \times 10^{-8} \text{W} \text{ m}^{-2} \text{K}^{-4}$	space	μ_0	$4\pi \times 10^{-7} \mathrm{H}\mathrm{m}^{-1}$
Universal constant			Speed of light in		
of gravitation	G	$6.67 \times 10^{-11} \mathrm{m^3 kg^{-1} s^{-2}}$	vacuum	С	$3.0 \times 10^8 \mathrm{ms^{-1}}$
			Speed of sound in		
			air	v	$3.4 \times 10^2 \mathrm{ms^{-1}}$

REFRACTIVE INDICES

The refractive indices refer to sodium light of wavelength 589 nm and to substances at a temperature of 273 K.

Substance	Refractive index	Substance	Refractive index
Diamond	2·42	Glycerol	1·47
Glass	1·51	Water	1·33
lce	1·31	Air	1∙00
Perspex	1·49	Magnesium Fluoride	1∙38

SPECTRAL LINES

Element	<i>Wavelength</i> /nm	Colour	Element	<i>Wavelength</i> /nm	Colour
Hydrogen	656 486 434	Red Blue-green Blue-violet	Cadmium	644 509 480	Red Green Blue
	410	Violet	Lasers		
	397	Ultraviolet	Element	Wavelength/nm	Colour
	389	Ultraviolet	Carbon dioxide	9550 7	Infrared
Sodium	589	Yellow	Helium-neon	10590) 633	Red

PROPERTIES OF SELECTED MATERIALS

Substance	<i>Density/</i> kg m ⁻³	Melting Point/ K	Boiling Point/ K	Specific Heat Capacity/ J kg ⁻¹ K ⁻¹	Specific Latent Heat of Fusion/ J kg ⁻¹	Specific Latent Heat of Vaporisation/ J kg ⁻¹
Aluminium	2·70 × 10 ³	933	2623	9.02 × 10 ²	3∙95 × 10⁵	
Copper	8∙96 × 10 ³	1357	2853	3⋅86 × 10 ²	2·05 × 10⁵	
Glass	2.60 × 10 ³	1400		6∙70 × 10 ²		
Ice	9∙20 × 10 ²	273		2.10 × 10 ³	3∙34 × 10 ⁵	
Glycerol	1·26 × 10 ³	291	563	2·43 × 10 ³	1∙81 × 10 ⁵	8∙30 × 10 ⁵
Methanol	7∙91 × 10 ²	175	338	2∙52 × 10 ³	9∙9 × 10 ⁴	1·12 × 10 ⁶
Sea Water	1.02 × 10 ³	264	377	3⋅93 × 10 ³		
Water	1.00 × 10 ³	273	373	4⋅19 × 10 ³	3∙34 × 10 ⁵	2·26 × 10 ⁶
Air	1.29					
Hydrogen	9·0 × 10 ^{−2}	14	20	1·43 × 10 ⁴		4∙50 × 10 ⁵
Nitrogen	1.25	63	77	1∙04 × 10 ³		2.00 × 10 ⁵
Oxygen	1.43	55	90	9·18 × 10 ²		2·40 × 10 ⁴

The gas densities refer to a temperature of 273 K and a pressure of 1.01×10^5 Pa.



Total marks — 140 marks Attempt ALL questions

1.



A car on a long straight track accelerates from rest. The car's run begins at time t = 0.

Its velocity v at time t is given by the equation

$$v = \mathbf{0} \cdot \mathbf{135}t^2 + \mathbf{1} \cdot \mathbf{26}t$$

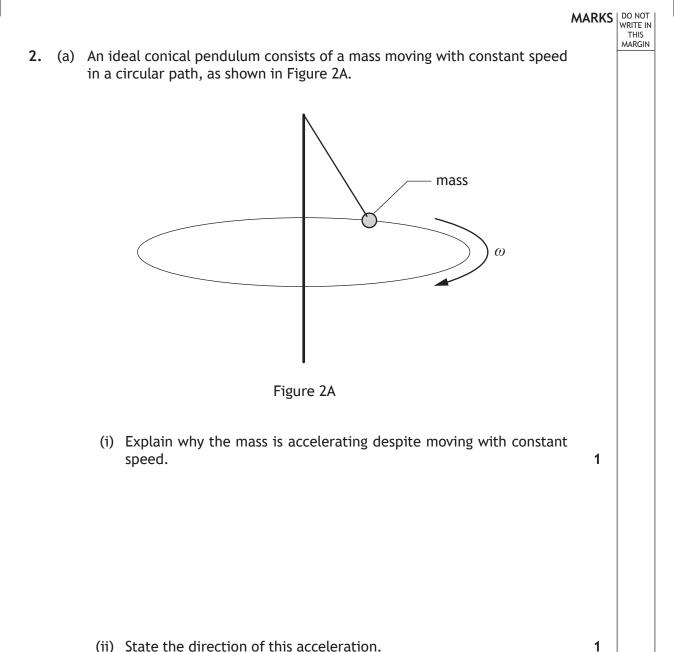
where v is measured in m s⁻¹ and t is measured in s. Using **calculus** methods:

(a) determine the acceleration of the car at $t = 15 \cdot 0$ s; Space for working and answer 3

3

(b) determine the displacement of the car from its original position at this time.
 Space for working and answer





(ii) State the direction of this acceleration.

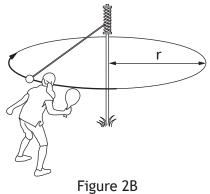


2. (continued)

(b) Swingball is a garden game in which a ball is attached to a light string connected to a vertical pole as shown in Figure 2B.

The motion of the ball can be modelled as a conical pendulum.

The ball has a mass of 0.059 kg.



ligure 20

(i) The ball is hit such that it moves with constant speed in a horizontal circle of radius 0.48 m.

The ball completes 1.5 revolutions in 2.69 s.

(A) Show that the angular velocity of the ball is 3.5 rad s^{-1} . Space for working and answer 2

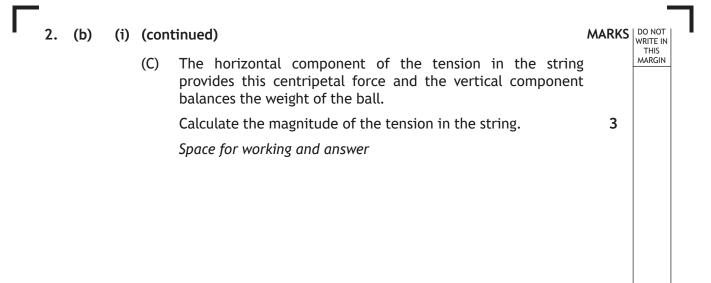
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 (B) Calculate the magnitude of the centripetal force acting on the ball.
 Space for working and answer







(ii) The string breaks whilst the ball is at the position shown in Figure 2C.

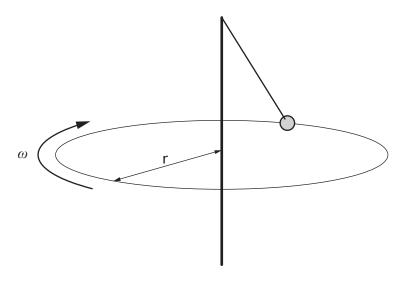


Figure 2C

On Figure 2C, draw the direction of the ball's velocity **immediately** after the string breaks.

1

(An additional diagram, if required, can be found on Page 39.)



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3. A spacecraft is orbiting a comet as shown in Figure 3.

The comet can be considered as a sphere with a radius of $2\cdot1\times10^3\,m$ and a mass of $9\cdot5\times10^{12}\,kg.$

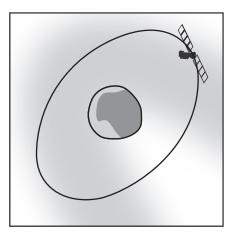


Figure 3 (not to scale)

(a) A lander was released by the spacecraft to land on the surface of the comet. After impact with the comet, the lander bounced back from the surface with an initial upward vertical velocity of 0.38 m s^{-1} .

By calculating the escape velocity of the comet, show that the lander returned to the surface for a second time.

Space for working and answer



3. (continued)

(b) (i) Show that the gravitational field strength at the surface of the comet is $1.4 \times 10^{-4} \,\text{N kg}^{-1}$. Space for working and answer

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(ii) Using the data from the space mission, a student tries to calculate the maximum height reached by the lander after its first bounce.

The student's working is shown below

 $v^{2} = u^{2} + 2as$ $0 = 0.38^{2} + 2 \times (-1.4 \times 10^{-4}) \times s$ s = 515.7 m

The actual maximum height reached by the lander was **not** as calculated by the student.

State whether the actual maximum height reached would be greater or smaller than calculated by the student.

You must justify your answer.



- MARKS DO NOT WRITE IN THIS MARGIN
- 4. Epsilon Eridani is a star 9.94×10^{16} m from Earth. It has a diameter of 1.02×10^{9} m. The apparent brightness of Epsilon Eridani is measured on Earth to be 1.05×10^{-9} W m⁻².

3

(a) Calculate the luminosity of Epsilon Eridani. Space for working and answer

(b) Calculate the surface temperature of Epsilon Eridani. Space for working and answer 3

(c) State an assumption made in your calculation in (b).



- 5. Einstein's theory of general relativity can be used to describe the motion of objects in non-inertial frames of reference. The equivalence principle is a key assumption of general relativity.
 - (a) Explain what is meant by the terms:
 - (i) non-inertial frames of reference;
 - (ii) the equivalence principle.

- (b) Two astronauts are on board a spacecraft in deep space far away from any large masses. When the spacecraft is accelerating one astronaut throws a ball towards the other.
 - (i) On Figure 5A sketch the path that the ball would follow in the astronauts' frame of reference.

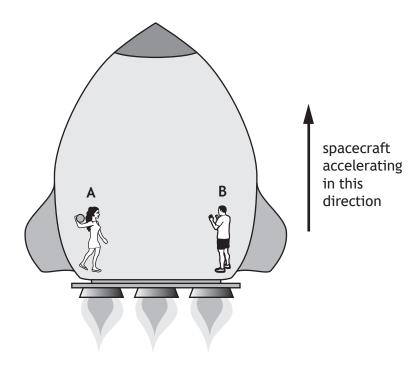


Figure 5A

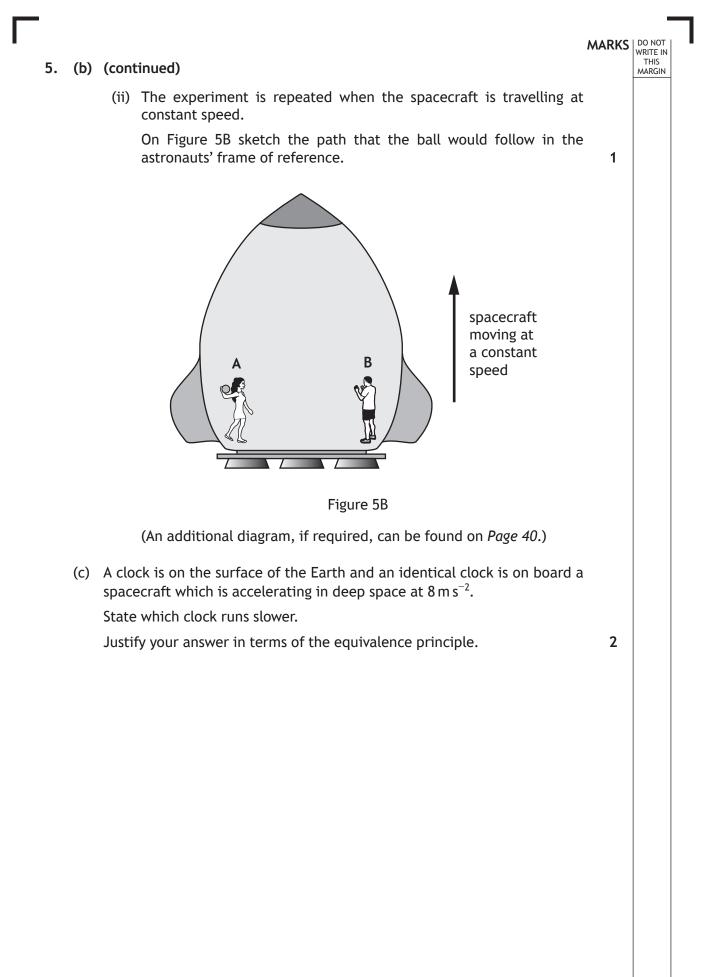
(An additional diagram, if required, can be found on Page 39.)



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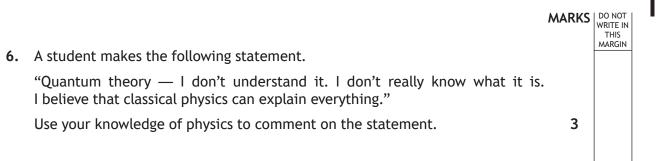
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7. (a) The Earth can be modelled as a black body radiator.

The average surface temperature of the Earth can be estimated using the relationship

$$T = \frac{b}{\lambda_{\text{peak}}}$$

where

T is the average surface temperature of the Earth in kelvin;

b is Wien's Displacement Constant equal to $2 \cdot 89 \times 10^{-3}$ K m;

 λ_{peak} is the peak wavelength of the radiation emitted by a black body radiator.

The average surface temperature of Earth is 15 °C.

(i) Estimate the peak wavelength of the radiation emitted by Earth. Space for working and answer

(ii) To which part of the electromagnetic spectrum does this peak wavelength correspond?

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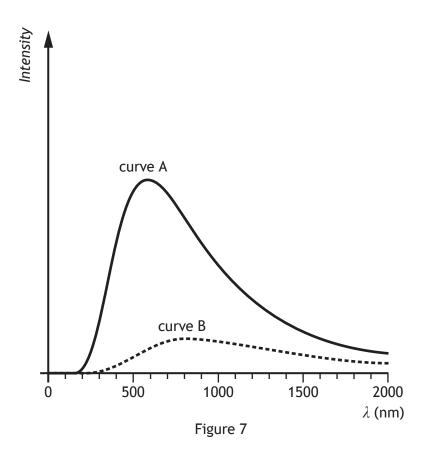


7. (continued)

(b) In order to investigate the properties of black body radiators a student makes measurements from the spectra produced by a filament lamp. Measurements are made when the lamp is operated at its rated voltage and when it is operated at a lower voltage.

The filament lamp can be considered to be a black body radiator.

A graph of the results obtained is shown in Figure 7.



(i) State which curve corresponds to the radiation emitted when the filament lamp is operating at its rated voltage.

You must justify your answer.

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(ii) The shape of the curves on the graph on Figure 7 is not as predicted by classical physics.

On Figure 7, sketch a curve to show the result predicted by classical physics.

(An additional graph, if required, can be found on Page 40.)



8. Werner Heisenberg is considered to be one of the pioneers of quantum mechanics.

He is most famous for his uncertainty principle which can be expressed in the equation

$$\Delta x \Delta p_x \ge \frac{h}{4\pi}$$

- (a) (i) State what quantity is represented by the term Δp_x .
 - (ii) Explain the implications of the Heisenberg uncertainty principle for experimental measurements.

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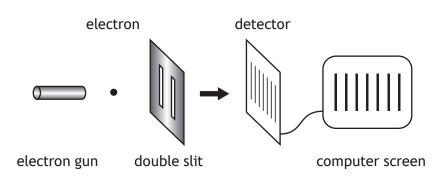


8. (continued)

(b) In an experiment to investigate the nature of particles, individual electrons were fired one at a time from an electron gun through a narrow double slit. The position where each electron struck the detector was recorded and displayed on a computer screen.

The experiment continued until a clear pattern emerged on the screen as shown in Figure 8.

The momentum of each electron at the double slit is 6.5×10^{-24} kg m s⁻¹.





not to scale

(i) The experimenter had three different double slits with slit separations 0.1 mm, $0.1 \mu \text{m}$ and 0.1 nm.

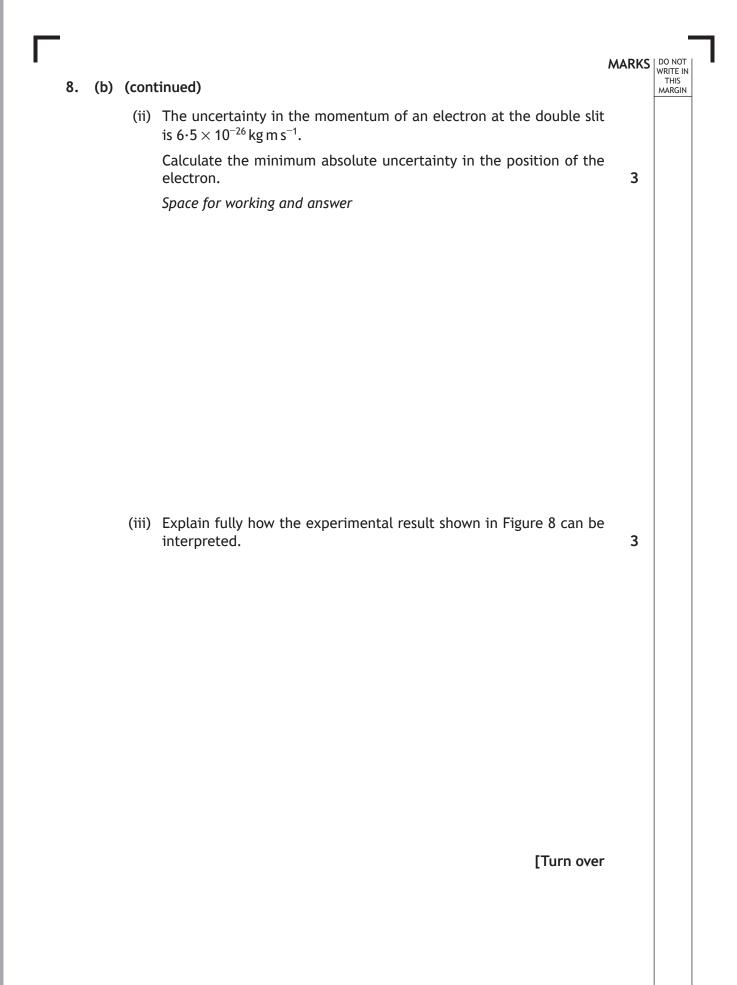
State which double slit was used to produce the image on the screen.

You must justify your answer by calculation of the de Broglie wavelength.

Space for working and answer



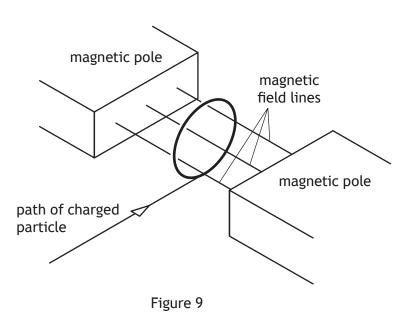
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9. A particle with charge q and mass m is travelling with constant speed v. The particle enters a uniform magnetic field at 90° and is forced to move in a circle of radius r as shown in Figure 9.

The magnetic induction of the field is B.



(a) Show that the radius of the circular path of the particle is given by

$$r = \frac{mv}{Bq}$$

2



9. (continued) MARKS DO NOT WRITE IN THIS MARGIN (b) In an experimental nuclear reactor, charged particles are contained in a magnetic field. One such particle is a deuteron consisting of one proton and one neutron. The kinetic energy of each deuteron is 1.50 MeV. The kinetic energy of each deuteron is 3.34×10^{-27} kg. Relativistic effects can be ignored. 4 (i) Calculate the speed of the deuteron. 4 Space for working and answer 4

(ii) Calculate the magnetic induction required to keep the deuteron moving in a circular path of radius 2.50 m.
 Space for working and answer

2



9. (b) (continued)

(iii) Deuterons are fused together in the reactor to produce isotopes of helium.

 ^3_2He nuclei, each comprising 2 protons and 1 neutron, are present in the reactor.

 A_2^{3} He nucleus also moves in a circular path in the same magnetic field.

The ${}_{2}^{3}$ He nucleus moves at the same speed as the deuteron.

State whether the radius of the circular path of the ${}_{2}^{3}$ He nucleus is greater than, equal to or less than 2.50 m.

You must justify your answer.

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10. (a) (i) State what is meant by *simple harmonic motion*.

(ii) The displacement of an oscillating object can be described by the expression

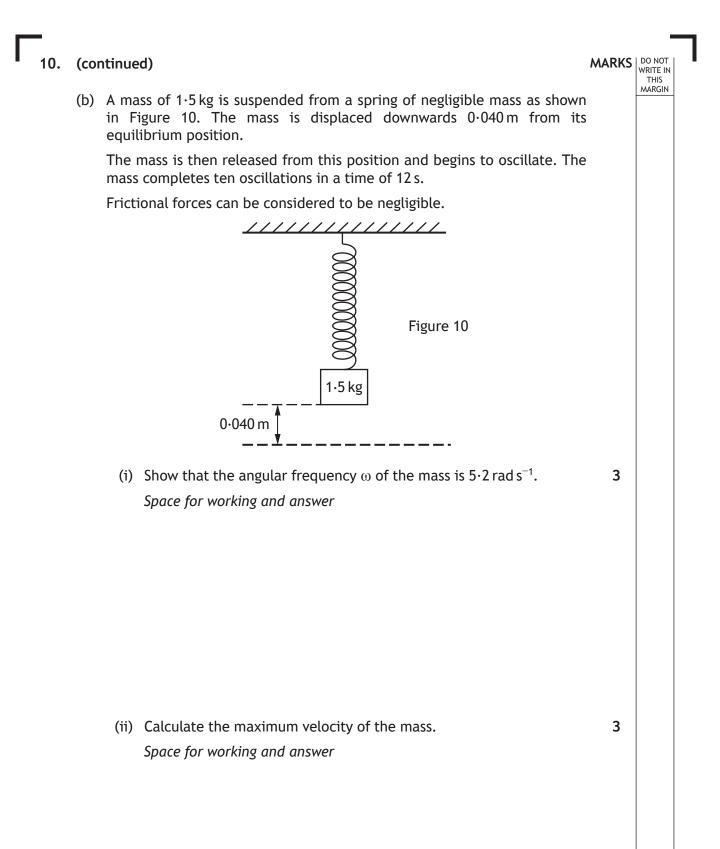
 $y = A\cos\omega t$

where the symbols have their usual meaning. Show that this expression is a solution to the equation

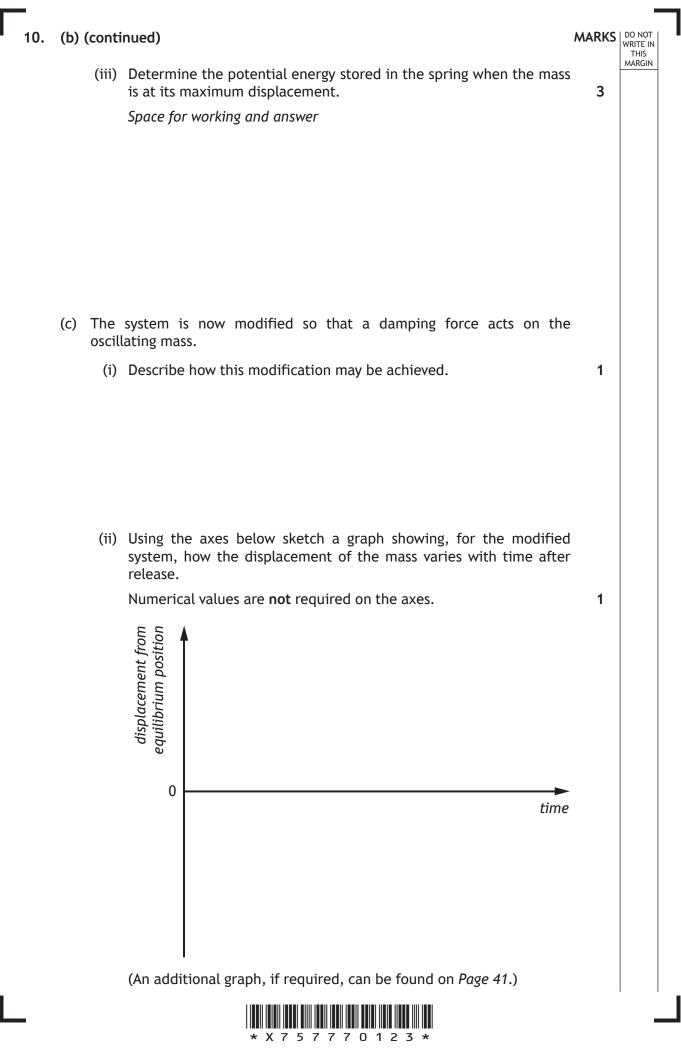
$$\frac{d^2 y}{dt^2} + \omega^2 y = \mathbf{0}$$

2



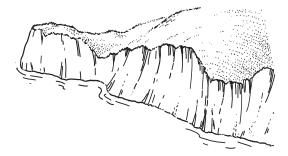






Page 23

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A ship emits a blast of sound from its foghorn. The sound wave is described by the equation

 $y = 0.250 \sin 2\pi (118t - 0.357x)$

where the symbols have their usual meaning.

(a) Determine the speed of the sound wave.Space for working and answer



11. (continued) MARKS DO NOT WRITE IN THIS MARGIN (b) The sound from the ship's foghorn reflects from a cliff. When it reaches the ship this reflected sound has half the energy of the original sound. Write an equation describing the reflected sound wave at this point. 4



12. Some early 3D video cameras recorded two separate images at the same time to create two almost identical movies.

Cinemas showed 3D films by projecting these two images simultaneously onto the same screen using two projectors. Each projector had a polarising filter through which the light passed as shown in Figure 12.

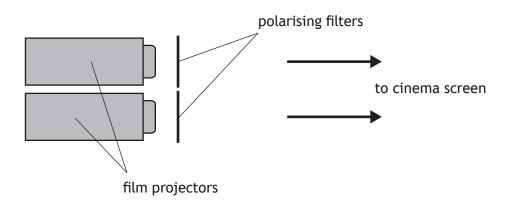


Figure 12

- (a) Describe how the transmission axes of the two polarising filters should be arranged so that the two images on the screen do not interfere with each other.
- (b) A student watches a 3D movie using a pair of glasses which contains two polarising filters, one for each eye.

Explain how this arrangement enables a different image to be seen by each eye.

2

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12. (continued)

(c) Before the film starts, the student looks at a ceiling lamp through one of the filters in the glasses. While looking at the lamp, the student then rotates the filter through 90°.

State what effect, if any, this rotation will have on the observed brightness of the lamp.

Justify your answer.

(d) During the film, the student looks at the screen through only one of the filters in the glasses. The student then rotates the filter through 90° and does not observe any change in brightness.

Explain this observation.

1

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Page 27

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MARKS MARKS UNDER THIS MARKS (a) Q_1 is a point charge of +12 nC. Point Y is 0.30 m from Q_1 as shown in Figure 13A.

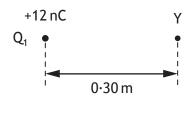


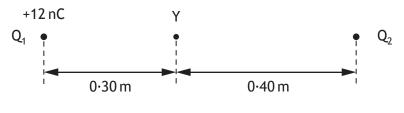
Figure 13A

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Show that the electrical potential at point Y is +360 V. Space for working and answer

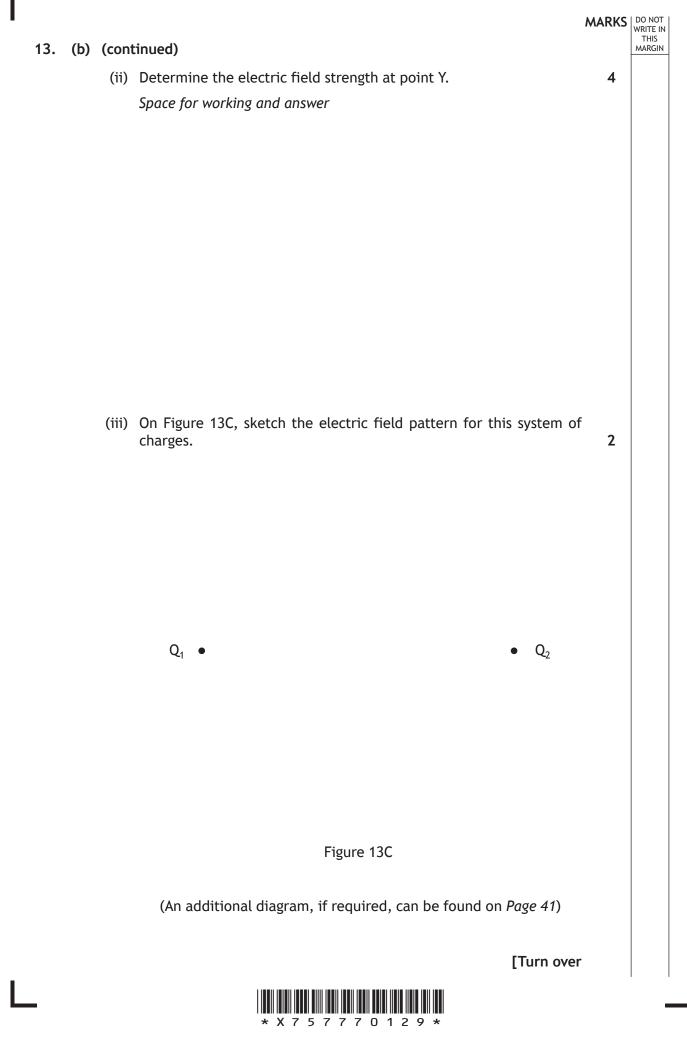
(b) A second point charge $\rm Q_2$ is placed at a distance of 0.40 m from point Y as shown in Figure 13B . The electrical potential at point Y is now zero.

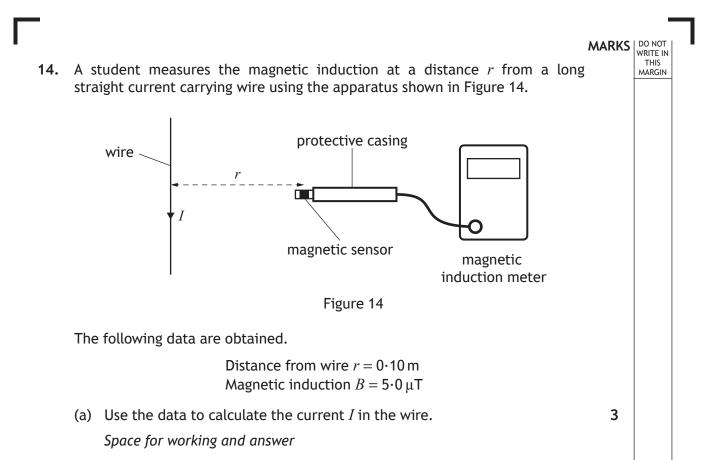




(i) Determine the charge of Q₂.Space for working and answer







(b) The student estimates the following uncertainties in the measurements of *B* and *r*.

Uncertainties	in r	Uncertainties	in <i>B</i>
reading	±0.002 m	reading	±0·1 μT
calibration	±0·0005 m	calibration	$\pm 1.5\%$ of reading

(i) Calculate the percentage uncertainty in the measurement of *r*. *Space for working and answer*

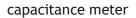


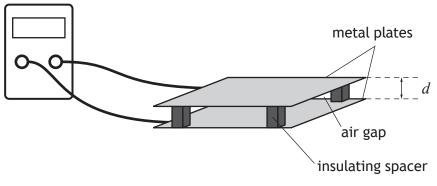
1	4.	(b)	(continued)	MARKS	DO NOT WRITE IN THIS MARGIN
			(ii) Calculate the percentage uncertainty in the measurement of <i>B</i>.Space for working and answer	3	
			(iii) Calculate the absolute uncertainty in the value of the current in the wire.Space for working and answer	2	
		(c)	The student measures distance r , as shown in Figure 14, using a metre stick. The smallest scale division on the metre stick is 1 mm. Suggest a reason why the student's estimate of the reading uncertainty in r is not ± 0.5 mm.	1	

[Turn over



15. A student constructs a simple air-insulated capacitor using two parallel metal plates, each of area A, separated by a distance *d*. The plates are separated using small insulating spacers as shown in Figure 15A.







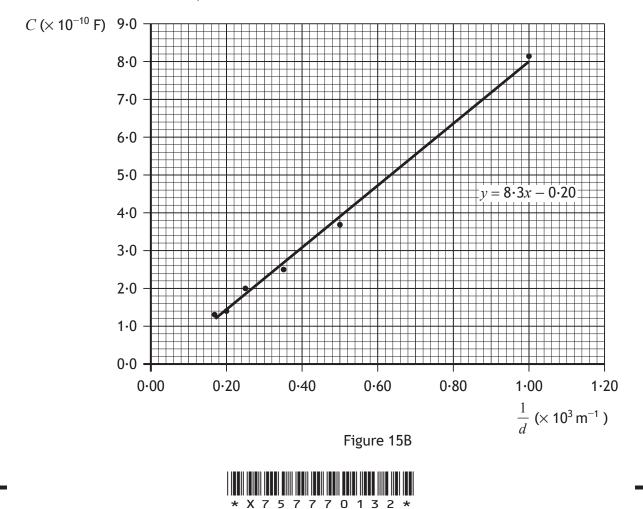
The capacitance C of the capacitor is given by

$$C = \varepsilon_0 \frac{A}{d}$$

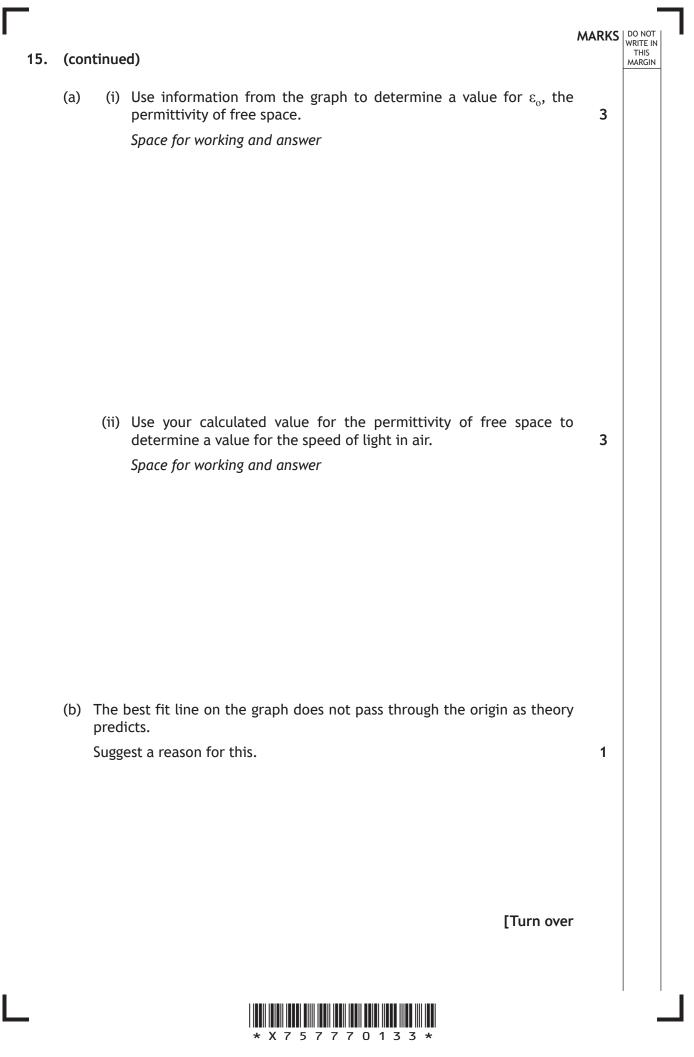
The student investigates how the capacitance depends on the separation of the plates. The student uses a capacitance meter to measure the capacitance for different plate separations. The plate separation is measured using a ruler.

The results are used to plot the graph shown in Figure 15B.

The area of each metal plate is $9 \cdot 0 \times 10^{-2} \text{ m}^2$.



Page 32



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 16. A student uses two methods to determine the moment of inertia of a solid sphere about an axis through its centre.
 MARGIN

 (a) In the first method the student measures the mass of the sphere to be 3.8 kg and the radius to be 0.053 m. Calculate the moment of inertia of the sphere.
 3

Space for working and answer

(b) In the second method, the student uses conservation of energy to determine the moment of inertia of the sphere.

The following equation describes the conservation of energy as the sphere rolls down the slope

$$mgh = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

where the symbols have their usual meanings.

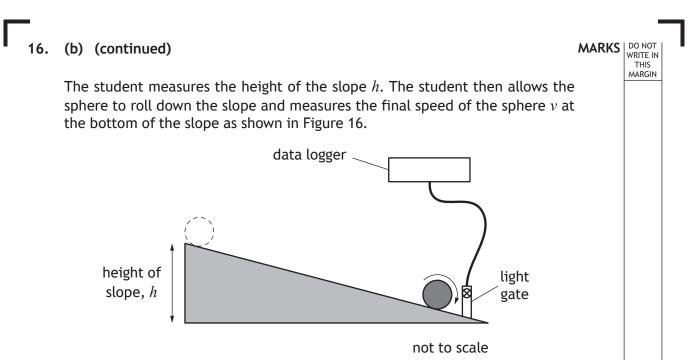
The equation can be rearranged to give the following expression

$$2gh = \left(\frac{I}{mr^2} + 1\right)v^2$$

This expression is in the form of the equation of a straight line through the origin,

$$y = gradient \times x$$







<i>h</i> (m)	$v ({\rm ms^{-1}})$	2gh (m ² s ⁻²)	v^2 (m ² s ⁻²)
0.020	0.42	0.39	0.18
0.040	0.63	0.78	0.40
0.060	0.68	1.18	0.46
0.080	0.95	1.57	0.90
0.100	1.05	1.96	1.10

The following is an extract from the student's notebook.

 $m = 3.8 \,\mathrm{kg}$ $r = 0.053 \,\mathrm{m}$

(i) On the square-ruled paper on *Page 37*, draw a graph that would allow the student to determine the moment of inertia of the sphere.

3

3

(ii) Use the gradient of your line to determine the moment of inertia of the sphere.

Space for working and answer



(An additional square-ruled paper, if required, can be found on Page 42.)



[Turn over for next question

16. (continued)

(c) The student states that more confidence should be placed in the value obtained for the moment of inertia in the second method.

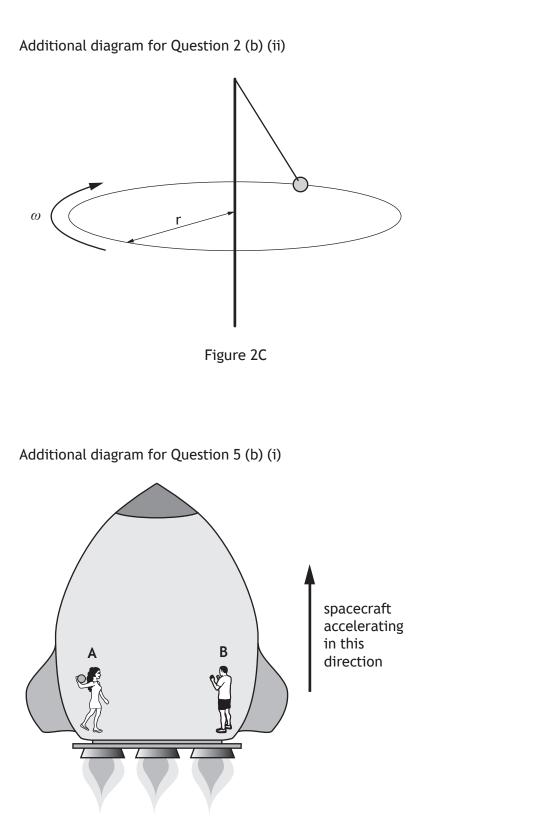
Use your knowledge of experimental physics to comment on the student's statement.

3

[END OF QUESTION PAPER]



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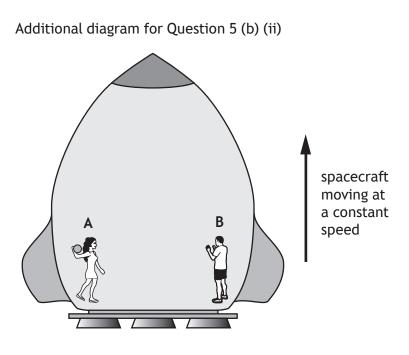
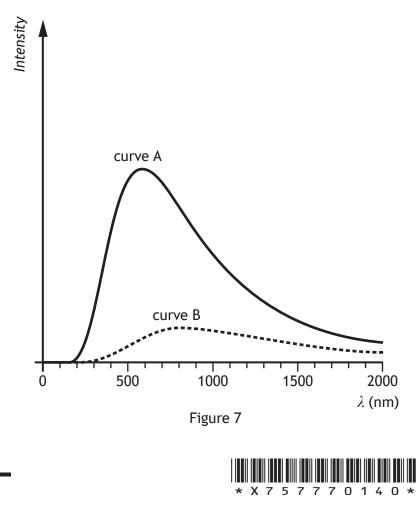
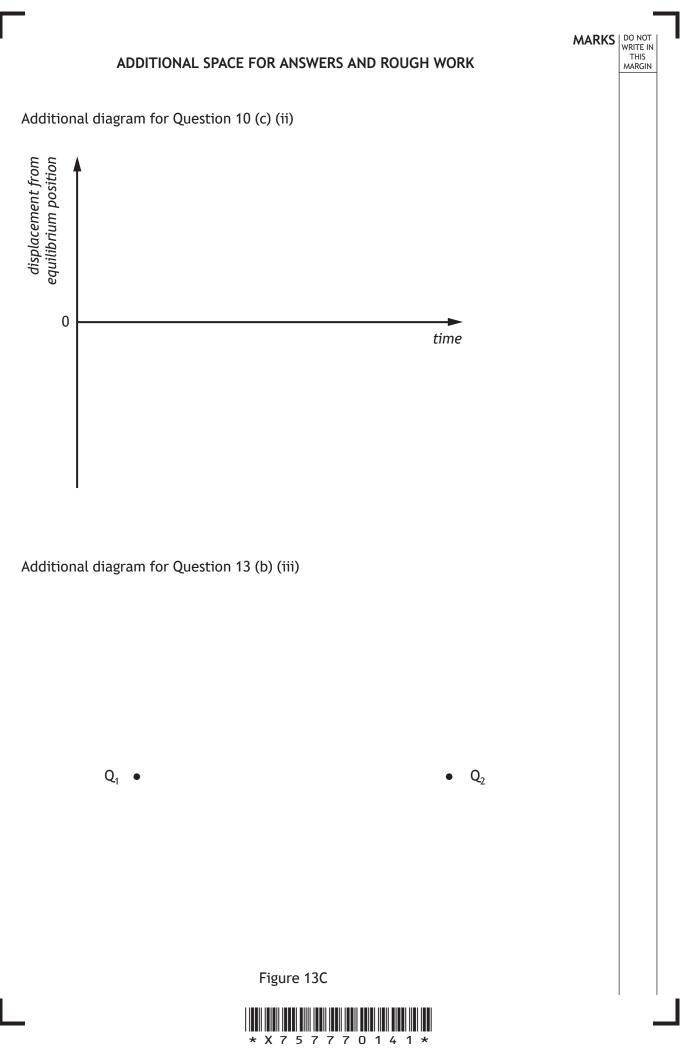
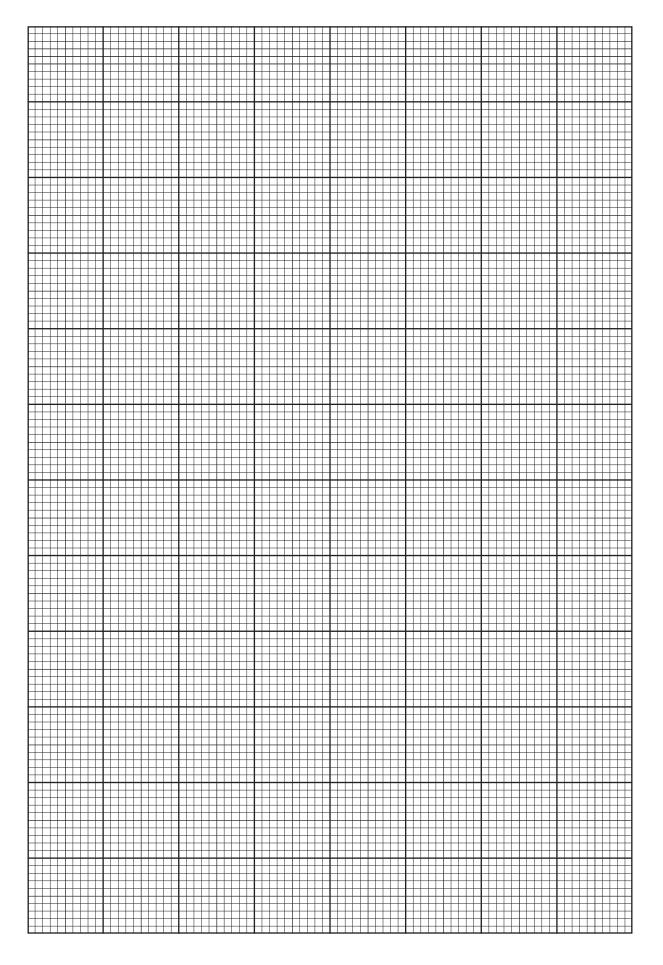


Figure 5B

Additional diagram for Question 7 (b) (ii)









ADDITIONAL SPACE FOR ANSWERS AND ROUGH WORK

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ADDITIONAL SPACE FOR ANSWERS AND ROUGH WORK



ACKNOWLEDGEMENT

Question 1 – Calvin Chan/shutterstock.com





National Qualifications 2016

X757/77/11

Physics Relationships Sheet

TUESDAY, 24 MAY 9:00 AM – 11:30 AM





$$\begin{aligned} v = \frac{ds}{dt} & L = I\omega \\ a = \frac{dv}{dt} = \frac{d^2s}{dt^2} & E_K = \frac{1}{2}I\omega^2 \\ v = u + at & F = G\frac{Mm}{r^2} \\ s = ut + \frac{1}{2}at^2 & V = -\frac{GM}{r} \\ v^2 = u^2 + 2as & v = \sqrt{\frac{2GM}{r}} \\ \omega = \frac{d\theta}{dt} & apparent brightness, b = \frac{L}{4\pi^{r^2}} \\ \alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2} & Power per unit area = \sigma T^4 \\ \omega = \omega_o t + \frac{1}{2}\alpha^2 & r_{softwaresoluld} = \frac{2GM}{c^2} \\ \omega^2 = \omega_o^2 + 2\alpha\theta & E = hf \\ s = r\theta & \lambda = \frac{h}{p} \\ v = r\omega \\ a_r = r\alpha & mvr = \frac{nh}{2\pi} \\ a_r = \frac{v^2}{r} = r\omega^2 & \Delta x \Delta p_x \ge \frac{h}{4\pi} \\ F = \frac{mv^2}{r} = mr\omega^2 & \Delta E \Delta t \ge \frac{h}{4\pi} \\ T = Fr & F = qvB \\ T = I\alpha & \omega = 2\pi f \\ L = mvr = mr^2\omega & a = \frac{d^2y}{dt^2} = -\omega^2y \end{aligned}$$

$$y = A \cos \omega \quad \text{or} \quad y = A \sin \omega \quad c = \frac{1}{\sqrt{k_o} \mu_o}$$

$$v = \pm \omega \sqrt{(A^2 - y^2)} \quad t = RC$$

$$E_\kappa = \frac{1}{2} m \omega^2 y^2 \quad X_c = \frac{1}{2} m \omega^2 y^2$$

$$y = A \sin 2\pi (ft - \frac{x}{\lambda}) \quad \mathcal{E} = -L \frac{dI}{dt}$$

$$E = kA^2 \quad \mathcal{E} = \frac{1}{2} LI^2$$

$$\phi = \frac{2\pi x}{\lambda} \quad X_L = \frac{V}{I}$$
optical path difference = $m\lambda$ or $\left(m + \frac{1}{2}\right)\lambda$
where $m = 0, 1, 2...$

$$\Delta x = \frac{\lambda I}{2d} \quad \Delta W = \sqrt{\Delta X^2 + \Delta Y^2 + \Delta Z^2}$$

$$\Delta x = \frac{\lambda D}{d}$$

$$n = \tan i_p$$

$$F = \frac{QQ_2}{4\pi \varepsilon_0 r^2}$$

$$F = QE$$

$$V = Ed$$

$$c = \frac{1}{\sqrt{k_o} \mu_o}$$

 $F = IlB\sin\theta$ $B = \frac{\mu_o I}{2\pi r}$

$$\begin{split} d = \overline{v}t & E_w = QV & V_{paak} = \sqrt{2}V_{rms} \\ s = \overline{v}t & E = mc^2 & I_{peak} = \sqrt{2}I_{rms} \\ v = u + at & E = hf & Q = It \\ s = ut + \frac{1}{2}at^2 & E_k = hf - hf_0 & V = IR \\ v^2 = u^2 + 2as & E_2 - E_1 = hf & P = IV = I^2R = \frac{V^2}{R} \\ s = \frac{1}{2}(u + v)t & T = \frac{1}{f} & R_T = R_1 + R_2 + \dots \\ W = mg & v = f\lambda & \frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots \\ F = ma & d\sin\theta = m\lambda & E = V + Ir \\ E_w = Fd & n = \frac{\sin\theta_1}{\sin\theta_2} & V_1 = \left(\frac{R_1}{R_1 + R_2}\right)V_s \\ E_p = mgh & \frac{\sin\theta_1}{\sin\theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} & \frac{V_1}{v_2} = \frac{R_1}{R_2} \\ E_K = \frac{1}{2}mv^2 & \sin\theta_c = \frac{1}{n} & C = \frac{Q}{V} \\ P = \frac{E}{t} & I = \frac{k}{d^2} & E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C} \end{split}$$

 $I = \frac{P}{A}$

path difference = $m\lambda$ or $\left(m + \frac{1}{2}\right)\lambda$ where m = 0, 1, 2...

random uncertainty = $\frac{\text{max. value} - \text{min. value}}{\text{number of values}}$

$$p = mv$$

Ft = mv - mu $F = G \frac{Mm}{r^2}$ $t' = \frac{t}{\sqrt{1 - (v'_c)^2}}$ $l' = l\sqrt{1 - (v'_c)^2}$ $f_o = f_s \left(\frac{v}{v \pm v_s}\right)$ $z = \frac{\lambda_{observed} - \lambda_{rest}}{\lambda_{rest}}$ $z = \frac{v}{c}$ $v = H_0 d$

Additional Relationships

Circle

 $circumference = 2\pi r$

area = πr^2

Sphere

 $area = 4\pi r^2$

volume = $\frac{4}{3}\pi r^3$

Trigonometry

 $\sin \theta = \frac{opposite}{hypotenuse}$

 $\cos\theta = \frac{adjacent}{hypotenuse}$

 $\tan \theta = \frac{opposite}{adjacent}$

 $\sin^2\theta + \cos^2\theta = 1$

Moment of inertia

point mass $I = mr^2$

rod about centre $I = \frac{1}{12}ml^2$

rod about end $I = \frac{1}{3}ml^2$

disc about centre $I = \frac{1}{2}mr^2$

sphere about centre $I = \frac{2}{5}mr^2$

Table of standard derivatives

f(x)	f'(x)
sin <i>ax</i>	$a\cos ax$
cosax	$-a\sin ax$

Table of standard integrals

f(x)	$\int f(x)dx$
sin <i>ax</i>	$-\frac{1}{a}\cos ax + C$
cosax	$\frac{1}{a}\sin ax + C$

Group Group Group Group Group Group Group 3 5 7 1 2 4 6 0 (1) (18) Key 1 2 Atomic number Η He Symbol 2 1 **Electron arrangement** Hydrogen Helium (2) (13) (14) (15) (17) (16) Name 7 3 4 5 6 8 9 10 Li Be С B Ν 0 F Ne 2.1 2.2 2, 3 2,4 2, 5 2,6 2,7 2,8 Lithium Beryllium Boron Carbon Nitrogen Oxygen Fluorine Neon 12 14 17 18 11 **Transition Elements** 13 15 16 Na Mg Si Р S Cl Al Ar 2, 8, 1 2, 8, 2 2, 8, 3 2, 8, 4 2, 8, 5 2, 8, 6 2, 8, 7 2, 8, 8 Chlorine Sodium Magnesium Aluminium Silicon Phosphorus Sulphur Argon (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) 24 25 29 19 20 21 22 23 26 27 28 30 31 32 33 34 35 36 Κ Ca V Sc Ti Zn Cr Mn Fe Co Ni Cu Ga Ge As Se Br Kr 2, 8, 8, 1 2, 8, 8, 2 2, 8, 10, 2 2, 8, 18, 1 2, 8, 9, 2 2, 8, 13, 1 2, 8, 13, 2 2, 8, 14, 2 2, 8, 15, 2 2, 8, 16, 2 2, 8, 18, 2 2, 8, 18, 3 2, 8, 18, 4 2, 8, 18, 5 2, 8, 18, 7 2, 8, 18, 8 2, 8, 11, 2 2, 8, 18, 6 Potassium Calcium Scandium Titanium Vanadium Chromium Manganese Iron Cobalt Nickel Copper Zinc Gallium Germanium Arsenic Selenium Bromine Krypton 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 Rb Sr Y Zr Nb Mo Tc Ru Rh Pd Cd In Sb Те Ι Xe Ag Sn 2, 8, 18, 8, 1 2, 8, 18, 8, 2 2, 8, 18, 9, 2 2.8.18.10.2 2, 8, 18, 12, 1 2, 8, 18, 13, 1 2, 8, 18, 13, 2 2.8.18.15.1 2, 8, 18, 16, 1 , 8, 18, 18, 0 , 8, 18, 18, 1 2, 8, 18, 18, 2 2, 8, 18, 18, 3 2. 8. 18. 18. 4 2, 8, 18, 18, 5 2.8.18.18.6 2, 8, 18, 18, 7 2, 8, 18, 18, 8 Rubidium Zirconium Niobium Molybdenum Rhodium Palladium Silver Tin Tellurium Strontium Yttrium Technetium Ruthenium Cadmium Indium Antimony Iodine Xenon 55 56 57 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 Hf W Tl Bi Cs Та Os Pt Pb Po At Ba La Re Ir Au Hg Rn 2, 8, 18, 18, 2, 8, 18, 18, 2, 8, 18, 18, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32 2, 8, 18, 32, 2, 8, 18, 32, 8,1 8, 2 9,2 10, 2 11, 2 12, 2 13, 2 14, 2 15, 2 17, 1 18, 1 18, 2 18, 3 18, 4 18, 5 18,6 18, 7 18, 8 Caesium Barium Lanthanun Hafnium Tantalum Tungsten Rhenium Osmium Iridium Platinum Gold Mercury Thallium Lead Bismuth Polonium Astatine Radon 87 88 89 108 109 104 105 106 107 Fr Ra Rf Db Bh Hs Mt Ac Sg 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 2, 8, 18, 32, 18, 8, 1 18, 8, 2 18, 9, 2 32, 10, 2 32, 11, 2 32, 12, 2 32, 13, 2 32, 14, 2 32, 15, 2 Francium Radium Actinium Rutherfordiu Dubnium Seaborgium Bohrium Hassium Meitnerium

Electron Arrangements of Elements

Lanthanides	57 La 2, 8, 18, 18, 9, 2 Lanthanum	58 Ce 2, 8, 18, 20, 8, 2 Cerium	59 Pr 2, 8, 18, 21, 8, 2 Praseodymium	60 Nd 2, 8, 18, 22, 8, 2 Neodymium	61 Pm 2, 8, 18, 23, 8, 2 Promethium	62 Sm 2, 8, 18, 24, 8, 2 Samarium	63 Eu 2, 8, 18, 25, 8, 2 Europium	64 Gd 2, 8, 18, 25, 9, 2 Gadolinium	65 Tb 2, 8, 18, 27, 8, 2 Terbium	66 Dy 2, 8, 18, 28, 8, 2 Dysprosium	67 Ho 2, 8, 18, 29, 8, 2 Holmium	68 Er 2, 8, 18, 30, 8, 2 Erbium	69 Tm 2, 8, 18, 31, 8, 2 Thulium	70 Yb 2, 8, 18, 32, 8, 2 Ytterbium	71 Lu 2, 8, 18, 32, 9, 2 Lutetium	
Actinides	89 Ac 2, 8, 18, 32, 18, 9, 2 Actinium	18, 10, 2	91 Pa 2, 8, 18, 32, 20, 9, 2 Protactinium	92 U 2, 8, 18, 32, 21, 9, 2 Uranium	93 Np 2, 8, 18, 32, 22, 9, 2 Neptunium	94 Pu 2, 8, 18, 32, 24, 8, 2 Plutonium	95 Am 2, 8, 18, 32, 25, 8, 2 Americium	96 Cm 2, 8, 18, 32, 25, 9, 2 Curium	97 Bk 2, 8, 18, 32, 27, 8, 2 Berkelium	98 Cf 2, 8, 18, 32, 28, 8, 2 Californium	99 Es 2, 8, 18, 32, 29, 8, 2 Einsteinium	30, 8, 2	101 Md 2, 8, 18, 32, 31, 8, 2 Mendelevium	102 No 2, 8, 18, 32, 32, 8, 2 Nobelium	103 Lr 2, 8, 18, 32, 32, 9, 2 Lawrencium	

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