•						
	FOR OFFICIAL U	SE				
	National Qualifica 2018				Mark	
X757/77/01					Р	hysio
TUESDAY, 8 MAY				11		
9:00 AM – 11:30 AM				*	X7577	701
Fill in these boxes and r Full name of centre	ead what is print	ted below.	Town			
Forename(s)	Su	irname			Number	of seat
Date of birth Day Mont	h Year	Scottish	candidate	e number		

Total marks — 140

Attempt ALL questions.

Reference may be made to the Physics Relationships Sheet X757/77/11 and the Data Sheet on page 02.

Write your answers clearly in the spaces provided in this booklet. Additional space for answers and rough work is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting. Any rough work must be written in this booklet. You should score through your rough work when you have written your final copy.

Care should be taken to give an appropriate number of significant figures in the final answers to calculations.

Use blue or black ink.

Before leaving the examination room you must give this booklet to the Invigilator; if you do not, you may lose all the marks for this paper.





DATA SHEET

COMMON PHYSICAL QUANTITIES

Quantity	Symbol	Value	Quantity	Symbol	Value
Gravitational					
acceleration on Earth	g	9⋅8 m s ⁻²	Mass of electron	me	9·11 × 10 ^{−31} kg
Radius of Earth	R _E	6·4 × 10 ⁶ m	Charge on electron	e	-1.60×10^{-19} C
Mass of Earth	$M_{\rm E}$	6∙0 × 10 ²⁴ kg	Mass of neutron	m _n	1⋅675 × 10 ⁻²⁷ kg
Mass of Moon	M _M	7.3×10^{22} kg	Mass of proton	mp	1⋅673 × 10 ⁻²⁷ kg
Radius of Moon	R _M	1.7 × 10 ⁶ m	Mass of alpha particle	m_{α}	6∙645 × 10 ⁻²⁷ kg
Mean Radius of			Charge on alpha		
Moon Orbit		3∙84 × 10 ⁸ m	particle		3·20 × 10 ^{−19} C
Solar radius		6∙955 × 10 ⁸ m	Planck's constant	h	6∙63 × 10 ^{−34} J s
Mass of Sun		2·0 × 10 ³⁰ kg	Permittivity of free		
1 AU		1∙5 × 10 ¹¹ m	space	ε_0	$8.85 \times 10^{-12} \mathrm{Fm}^{-1}$
Stefan-Boltzmann			Permeability of free		
constant	σ	$5.67 \times 10^{-8} \mathrm{W}\mathrm{m}^{-2}\mathrm{K}^{-4}$	space	μ_0	$4\pi \times 10^{-7} \mathrm{H}\mathrm{m}^{-1}$
Universal constant			Speed of light in		
of gravitation	G	$6.67 \times 10^{-11} \mathrm{m^3 kg^{-1} s^{-2}}$	vacuum	С	$3.00 \times 10^8 \mathrm{ms^{-1}}$
			Speed of sound in		
			air	v	$3.4 \times 10^2 \mathrm{ms^{-1}}$

REFRACTIVE INDICES

The refractive indices refer to sodium light of wavelength 589 nm and to substances at a temperature of 273 K.

Substance	Refractive index	Substance	Refractive index
Diamond Glass Ice	2·42 1·51 1·31	Glycerol Water Air	1·47 1·33 1·00
Perspex	1.49	Magnesium Fluoride	1.38

SPECTRAL LINES

Element	<i>Wavelength</i> /nm	Colour	Element	Wavelength/nm	Colour
Hydrogen	656 486 434	Red Blue-green Blue-violet	Cadmium	644 509 480	Red Green Blue
	410	Violet	Lasers		
	397	Ultraviolet Ultraviolet	Element	Wavelength/nm	Colour
	389		Carbon dioxide	9550 7	Infrared
Sodium	589	Yellow	Helium-neon	10 590 5 633	Red

PROPERTIES OF SELECTED MATERIALS

Substance	<i>Density/</i> kg m ⁻³	Melting Point/ K	Boiling Point/ K	Specific Heat Capacity/ J kg ⁻¹ K ⁻¹	Specific Latent Heat of Fusion/ J kg ⁻¹	Specific Latent Heat of Vaporisation/ J kg ⁻¹
Aluminium	2·70 × 10 ³	933	2623	9.02 × 10 ²	3∙95 × 10⁵	
Copper	8∙96 × 10³	1357	2853	3⋅86 × 10 ²	2·05 × 10⁵	
Glass	2∙60 × 10 ³	1400		6∙70 × 10 ²		
Ice	9∙20 × 10²	273		2.10 × 10 ³	3∙34 × 10 ⁵	
Glycerol	1·26 × 10 ³	291	563	2·43 × 10 ³	1⋅81 × 10 ⁵	8∙30 × 10 ⁵
Methanol	7∙91 × 10 ²	175	338	2∙52 × 10 ³	9∙9 × 10 ⁴	1·12 × 10 ⁶
Sea Water	1.02 × 10 ³	264	377	3∙93 × 10 ³		
Water	1∙00 × 10³	273	373	4⋅18 × 10 ³	3∙34 × 10 ⁵	2·26 × 10 ⁶
Air	1.29					
Hydrogen	9·0 × 10 ^{−2}	14	20	1·43 × 10 ⁴		4∙50 × 10 ⁵
Nitrogen	1.25	63	77	1.04 × 10 ³		2.00 × 10 ⁵
Oxygen	1.43	55	90	9·18 × 10 ²		2.40×10^4

The gas densities refer to a temperature of 273 K and a pressure of 1.01×10^5 Pa.



1. Energy is stored in a clockwork toy car by winding-up an internal spring using a key. The car is shown in Figure 1A.



Figure 1A

The car is released on a horizontal surface and moves forward in a straight line. It eventually comes to rest.

The velocity v of the car, at time t after its release, is given by the relationship

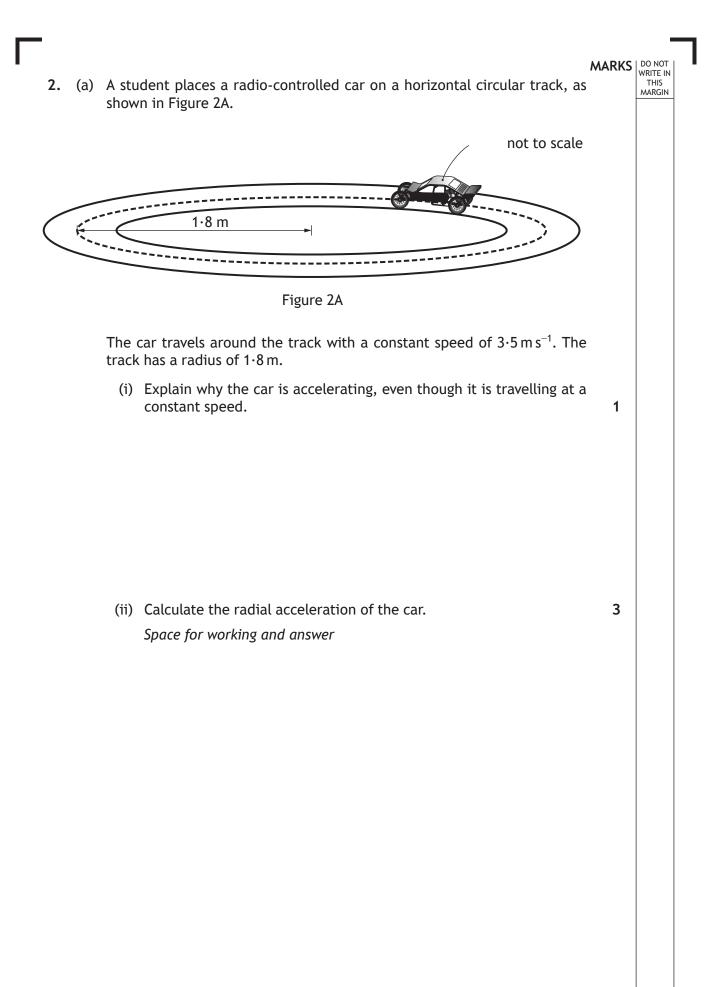
 $v = 0.0071t - 0.00025t^2$

where v is measured in m s⁻¹ and t is measured in s. Using calculus methods:

(a) determine the acceleration of the car 20.0 s after its release;
 Space for working and answer

(b) determine the distance travelled by the car 20.0 s after its release. Space for working and answer 3





* X 7 5 7 7 7 0 1 0 4 *

2. (a) (continued)

MARKS DO NOT WRITE IN THIS MARGIN

3

(iii) The car has a mass of 0.431 kg.

The student now increases the speed of the car to $5.5 \,\mathrm{m \, s^{-1}}$.

The total radial friction between the car and the track has a maximum value of 6.4 N.

Show by calculation that the car cannot continue to travel in a circular path.

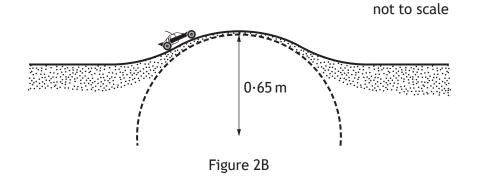
Space for working and answer



[Turn over

2. (continued)

(b) The car is now placed on a track, which includes a raised section. This is shown in Figure 2B.



The raised section of the track can be considered as the arc of a circle, which has radius r of 0.65 m.

(i) The car will lose contact with the raised section of track if its speed is greater than v_{max} .

Show that v_{max} is given by the relationship

$$v_{max} = \sqrt{gr}$$

(ii) Calculate the maximum speed v_{max} at which the car can cross the raised section without losing contact with the track.

Space for working and answer



page 06

2

2

MARKS DO NOT WRITE IN THIS MARGIN

2. (b) (continued)

(iii) A second car, with a smaller mass than the first car, approaches the raised section at the same speed as calculated in (b)(ii).

State whether the second car will lose contact with the track as it crosses the raised section.

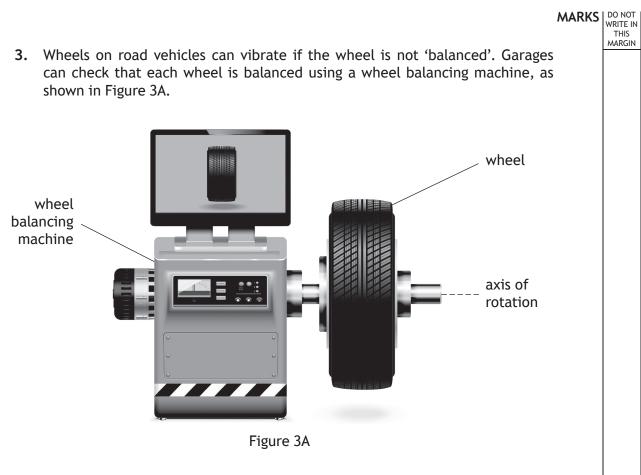
Justify your answer in terms of forces acting on the car.

[Turn over

MARKS DO NOT WRITE IN THIS MARGIN

2





The wheel is rotated about its axis by the wheel balancing machine.

The angular velocity of the wheel increases uniformly from rest with an angular acceleration of 6.7 rad s^{-2} .

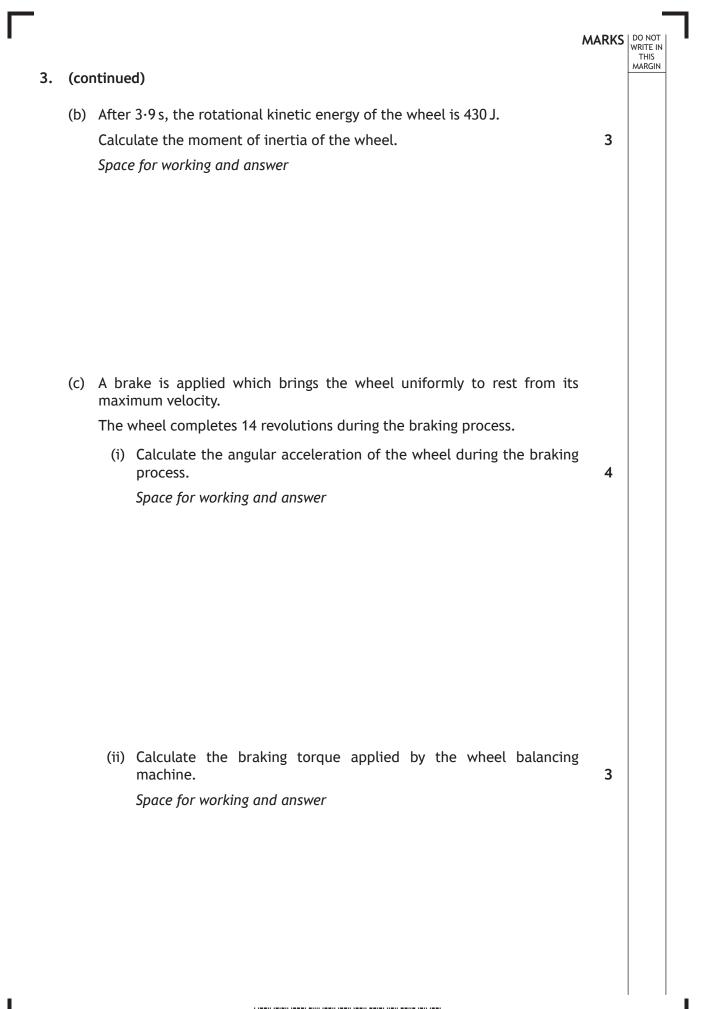
2

(a) The wheel reaches its maximum angular velocity after 3.9s.

Show that its maximum angular velocity is 26 rad s^{-1} .

Space for working and answer

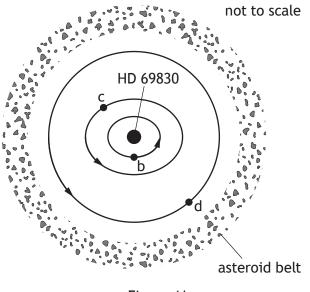
X 7 5 7 7 7 0 1 0 8 *



* X 7 5 7 7 7 0 1 0 9 *

4. Astronomers have discovered another solar system in our galaxy. The main sequence star, HD 69830, lies at the centre of this solar system. This solar system also includes three exoplanets, b, c, and d and an asteroid belt.

This solar system is shown in Figure 4A.



- Figure 4A
- (a) The orbit of exoplanet d can be considered circular.

To a reasonable approximation the centripetal force on exoplanet d is provided by the gravitational attraction of star HD 69830.

(i) Show that, for a circular orbit of radius r, the period T of a planet about a parent star of mass M, is given by

$$T^2 = \frac{4\pi^2}{GM}r^3$$



MARKS DO NOT WRITE IN THIS MARGIN

4. (a) (continued)

(ii) Some information about this solar system is shown in the table below.

Exoplanet	Type of orbit	Mass in Earth masses	Mean orbital radius in Astronomical Units (AU)	Orbital period In Earth days
b	Elliptical	10.2	-	8.67
с	Elliptical	11.8	0.186	-
d	Circular	18.1	0.63	197

Determine the mass, in kg, of star HD 69830.

Space for working and answer

(b) Two asteroids collide at a distance of 1.58×10^{11} m from the centre of the star HD 69830. As a result of this collision, one of the asteroids escapes from this solar system.

Calculate the minimum speed which this asteroid must have immediately after the collision, in order to escape from this solar system.

3

Space for working and answer



MARKS DO NOT WRITE IN THIS MARGIN

5. (a) Explain what is meant by the term *Schwarzschild radius*.

(b) (i) Calculate the Schwarzschild radius of the Sun. Space for working and answer

(ii) Explain, with reference to its radius, why the Sun is not a black hole.

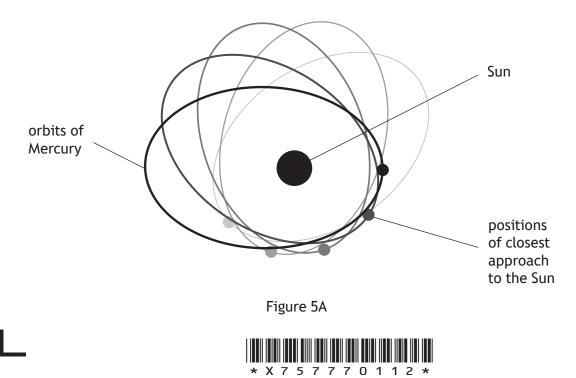
1

3

1

THIS

(c) The point of closest approach of a planet to the Sun is called the perihelion of the planet. The perihelion of Mercury rotates slowly around the Sun, as shown in Figure 5A.



5. (c) (continued)

This rotation of the perihelion is referred to as the precession of Mercury, and is due to the curvature of spacetime. This causes an angular change in the perihelion of Mercury.

The angular change per orbit is calculated using the relationship

$$\phi = 3\pi \frac{r_s}{a(1-e^2)}$$

where:

 ϕ is the angular change **per orbit**, in radians;

 r_s is the Schwarzschild radius of the Sun, in metres;

a is the semi-major axis of the orbit, for Mercury $a = 5.805 \times 10^{10} \text{ m}$;

e is the eccentricity of the orbit, for Mercury e = 0.206.

Mercury completes four orbits of the Sun in one Earth year.

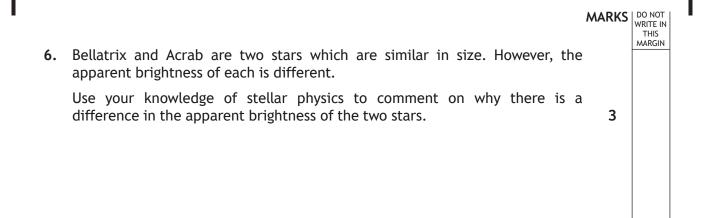
Determine the angular change in the perihelion of Mercury **after one Earth year**.

Space for working and answer

* X 7 5 7 7 7 0 1 1 3 *



MARKS DO NOT WRITE IN THIS MARGIN

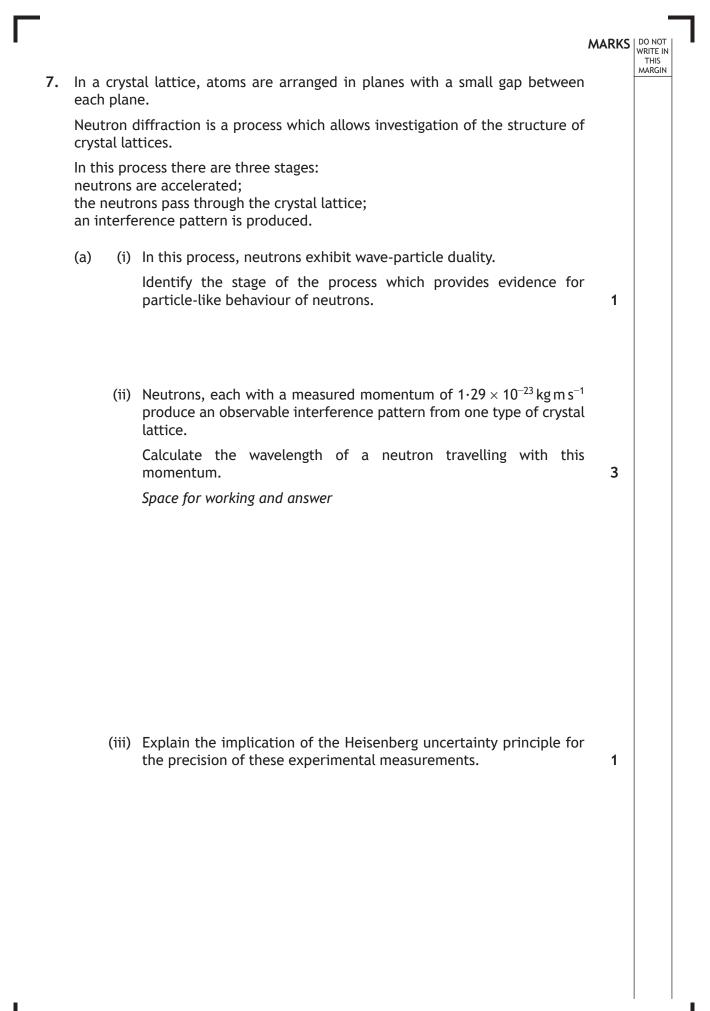




[Turn over for next question

DO NOT WRITE ON THIS PAGE







7. (a) (continued)

(iv) The momentum of a neutron is measured to be $1\cdot 29 \times 10^{-23}$ kg m s⁻¹ with a precision of $\pm 3\cdot 0\%$.

Determine the minimum **absolute** uncertainty in the position Δx_{min} of this neutron.

Space for working and answer

(b) Some of the neutrons used to investigate the structure of crystal lattices will not produce an observed interference pattern. This may be due to a large uncertainty in their momentum.

Explain why a large uncertainty in their momentum would result in these neutrons being unsuitable for this diffraction process.

2

MARKS DO NOT

4

THIS



MARKS DO NOT WRITE IN THIS MARGIN

1

2

8. (a) Inside the core of stars like the Sun, hydrogen nuclei fuse together to form heavier nuclei.

(i) State the region of the Hertzsprung-Russell diagram in which stars like the Sun are located.

(ii) One type of fusion reaction is known as the proton-proton chain and is described below.

$$6_{1}^{1}H \rightarrow {}_{2}^{4}X + 2_{1}^{0}Z + 2_{0}^{0}v + 2_{1}^{1}H + 2_{0}^{0}v$$

Identify the particles indicated by the letters X and Z.

(b) High energy charged particles are ejected from the Sun.State the name given to the constant stream of charged particles which the Sun ejects.



8. (continued)

(c) The stream of particles being ejected from the Sun produces an outward pressure. This outward pressure depends on the number of particles being ejected from the Sun and the speed of these particles.

The pressure at a distance of one astronomical unit (AU) from the Sun is given by the relationship

 $p = 1.6726 \times 10^{-6} \times n \times v^2$

where:

p is the pressure in nanopascals;

n is the number of particles per cubic centimetre;

v is the speed of particles in kilometres per second.

(i) On one occasion, a pressure of 9.56 × 10⁻¹⁰ Pa was recorded when the particle speed was measured to be 6.02 × 10⁵ m s⁻¹.
 Calculate the number of particles per cubic centimetre.
 Space for working and answer

(ii) The pressure decreases as the particles stream further from the Sun.

This is because the number of particles per cubic centimetre decreases and the kinetic energy of the particles decreases.

- (A) Explain why the number of particles per cubic centimetre decreases as the particles stream further from the Sun.
- (B) Explain why the kinetic energy of the particles decreases as the particles stream further from the Sun.

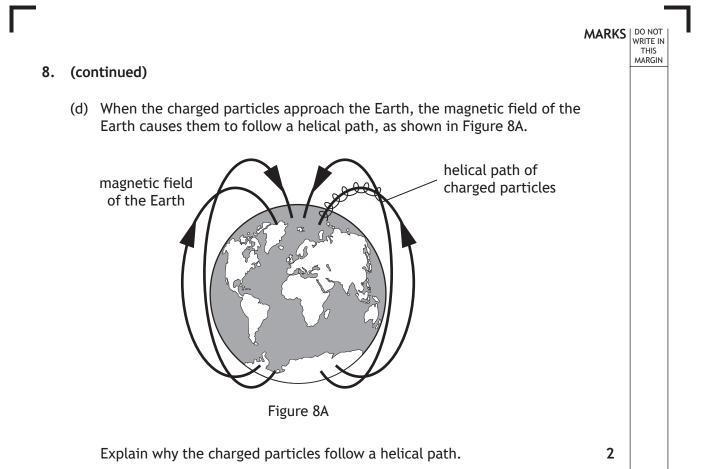


[Turn over

MARKS DO NOT WRITE IN THIS MARGIN

2

1





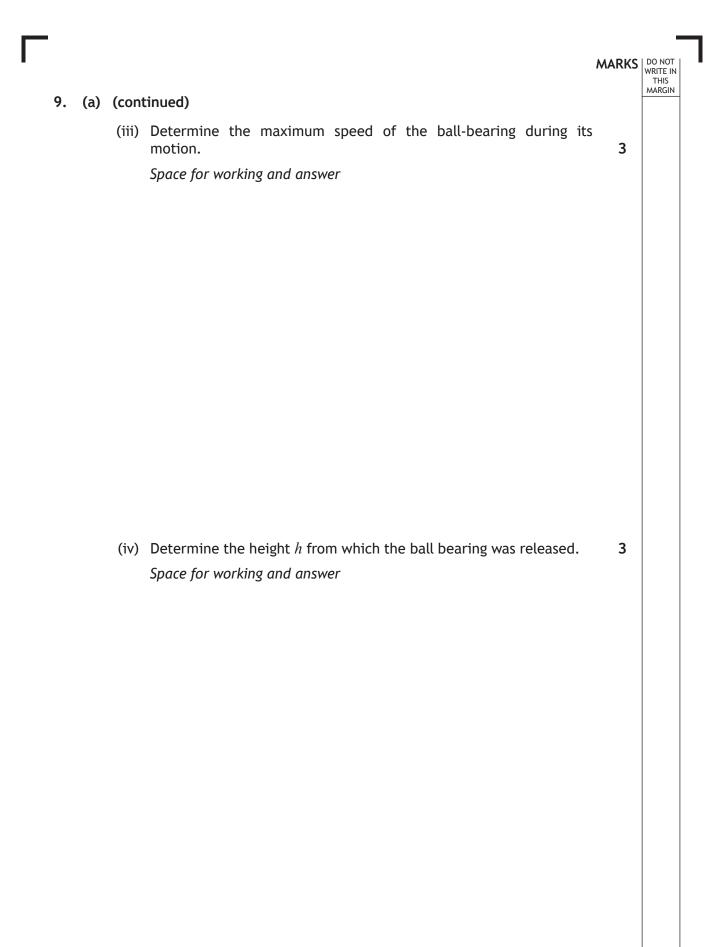
[Turn over for next question

DO NOT WRITE ON THIS PAGE



MARKS DO NOT THIS 9. A ball-bearing is released from height h on a smooth curved track, as shown in Figure 9A. The ball-bearing oscillates on the track about position P. The motion of the ball-bearing can be modelled as Simple Harmonic Motion (SHM). ball-bearing track h Ρ Figure 9A (a) The ball-bearing makes 1.5 oscillations in 2.5 s. (i) Show that the angular frequency of the ball-bearing is $3 \cdot 8 \text{ rad s}^{-1}$. 2 Space for working and answer (ii) The horizontal displacement x of the ball-bearing from position P at time t can be predicted using the relationship $x = -0.2\cos(3.8t)$ Using calculus methods, show that this relationship is consistent 3 with SHM.







MARKS DO NOT WRITE IN THIS MARGIN (continued) 9. (b) In practice, the maximum horizontal displacement of the ball-bearing decreases with time. A graph showing the variation in the horizontal displacement of the ball-bearing from position P with time is shown in Figure 9B. 0.25 horizontal displacement from position P (m) 0.20 0.15 0.10 0.05 0 time (s) -0.05-0.10- 0.15 - 0.20 - 0.25 0 0.50 1.00 1.50 2.00 2.50

Figure 9B

Sketch a graph showing how the **vertical** displacement of the ball-bearing from position P changes over the same time period.

2

Numerical values are not required on either axis.

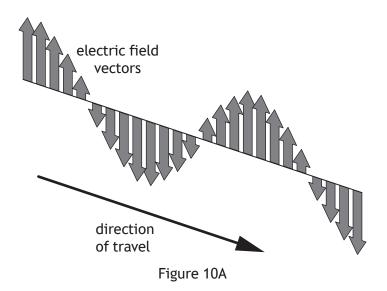


[Turn over for next question

DO NOT WRITE ON THIS PAGE



MARKS MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS
 MARKS



The direction of travel of the wave is taken to be the *x*-direction.

The magnitude of the electric field vector E at any point x and time t is given by the relationship

$$E = 12 \times 10^{-6} \sin 2\pi \left(1.31 \times 10^{14} t - \frac{x}{1.55 \times 10^{-6}} \right)$$

(a) (i) Two points, A and B, along the wave are separated by a distance of 4.25×10^{-7} m in the *x*-direction.

Calculate the phase difference between points A and B. Space for working and answer

3



THIS 10. (a) (continued) (ii) Another two points on the wave, P and Q, have a phase difference of π radians. State how the direction of the electric field vector at point P compares to the direction of the electric field vector at point Q. 1 (i) Show that the speed of the electromagnetic wave in this optical (b) fibre is $2.03 \times 10^8 \,\mathrm{m \, s^{-1}}$. 2 Space for working and answer (ii) The speed v_m of an electromagnetic wave in a medium is given by the relationship $v_m = \frac{1}{\sqrt{\varepsilon_m \mu_m}}$ The permeability μ_m of the optical fibre material can be considered to be equal to the permeability of free space. By considering the speed of the electromagnetic wave in this fibre, determine the permittivity ε_m of the optical fibre material. 2 Space for working and answer



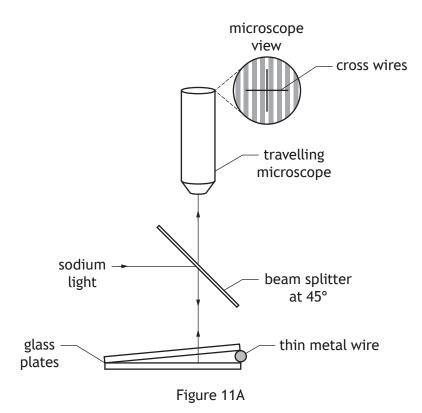
11. A thin air wedge is formed between two glass plates of length 75 mm, which are in contact at one end and separated by a thin metal wire at the other end.

DO NOT WRITE IN

THIS

Figure 11A shows sodium light being reflected down onto the air wedge.

A travelling microscope is used to view the resulting interference pattern.



A student observes the image shown in Figure 11B.

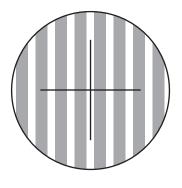
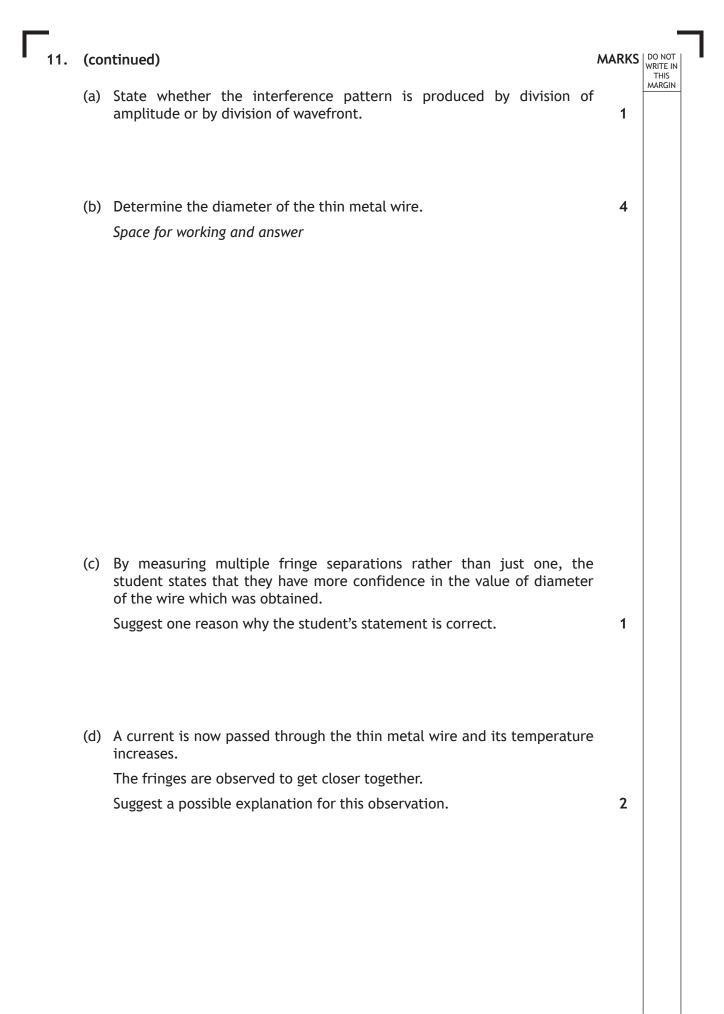


Figure 11B

The student aligns the cross-hairs to a bright fringe and then moves the travelling microscope until 20 further bright fringes have passed through the cross-hairs and notes that the travelling microscope has moved a distance of 9.8×10^{-4} m.

The student uses this data to determine the thickness of the thin metal wire between the glass plates.

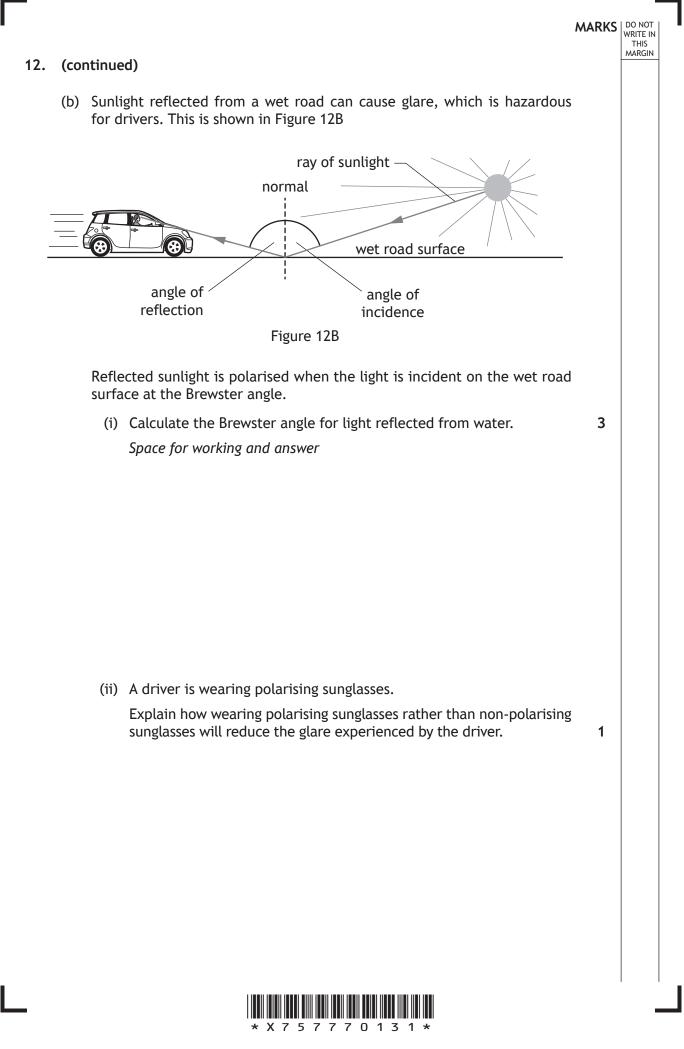






THIS **12.** A student is observing the effect of passing light through polarising filters. Two polarising filters, the polariser and the analyser, are placed between a lamp and the student as shown in Figure 12A. The polariser is held in a fixed position, and the analyser can be rotated. Angle θ is the angle between the transmission axes of the two filters. unpolarised light source analyser rotated θ through angle θ transmission axis of the polariser transmission axis of the analyser Figure 12A When the transmission axes of the polariser and the analyser are parallel, θ is 0° and the student observes bright light from the lamp. (a) (i) Describe, in terms of brightness, what the student observes as the 2 analyser is slowly rotated from 0° to 180°. (ii) The polariser is now removed. Describe, in terms of brightness, what the student observes as the analyser is again slowly rotated from 0° to 180° 1





13. (a) State what is meant by *electric field strength*.

(b) Two identical spheres, each with a charge of +22 nC, are suspended from point P by two equal lengths of light insulating thread.

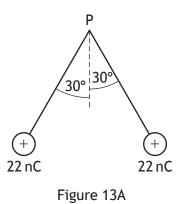
The spheres repel and come to rest in the positions shown in Figure 13A.

MARKS DO NOT

1

2

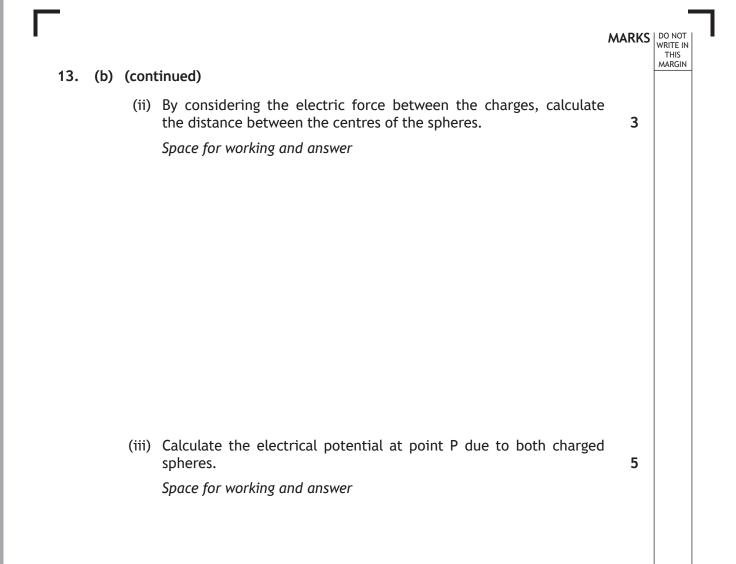
THIS



(i) Each sphere has a weight of 9.80×10^{-4} N.

By considering the forces acting on one of the spheres, show that the electric force between the charges is $5 \cdot 66 \times 10^{-4}$ N. Space for working and answer







14. A student carries out an experiment to determine the charge to mass ratio of the electron.

DO NOT WRITE IN THIS MARGIN

Figure 14A

An electron beam is produced using an electron gun connected to a 5.0 kV supply. A current I in the Helmholtz coils produces a uniform magnetic field.

The electron beam enters the magnetic field.

The apparatus is set up as shown in Figure 14A.

The path of the electron beam between points O and P can be considered to be an arc of a circle of constant radius r. This is shown in Figure 14B.

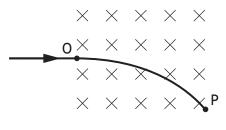


Figure 14B

The student records the following measurements:

Electron gun supply voltage, V	5∙0 kV (±10%)
Current in the Helmholtz coils, I	0·22 A (±5%)
Radius of curvature of the path of the electron beam between O and P, <i>r</i>	0·28 m (±6%)



14. (continued)MARKSDO NOT
WRITE IN
THIS
MARGIN(a) The manufacturer's instruction sheet states that the magnetic field
strength B at the centre of the apparatus is given by $B = 4 \cdot 20 \times 10^{-3} \times I$ $B = 4 \cdot 20 \times 10^{-3} \times I$ Calculate the magnitude of the magnetic field strength in the centre of
the apparatus.1Space for working and answer1

(b) The charge to mass ratio of the electron is calculated using the following relationship

$$\frac{q}{m} = \frac{2V}{B^2 r^2}$$

(i) Using the measurements recorded by the student, calculate the charge to mass ratio of the electron.

Space for working and answer

(ii) Determine the absolute uncertainty in the charge to mass ratio of the electron.

Space for working and answer



2

14. (continued)

- MARKS DO NOT WRITE IN THIS MARGIN
- (c) A second student uses the same equipment to find the charge to mass ratio of the electron and analyses their measurements differently.

The current in the Helmholtz coils is varied to give a range of values for magnetic field strength. This produces a corresponding range of measurements of the radius of curvature.

The student then draws a graph and uses the gradient of the line of best fit to determine the charge to mass ratio of the electron.

Suggest which quantities the student chose for the axes of the graph.



3

14. (continued)

(d) The graphical method of analysis used by the second student should give a more reliable value for the charge to mass ratio of the electron than the value obtained by the first student.

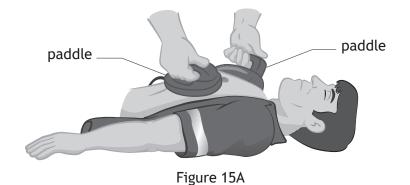
Use your knowledge of experimental physics to explain why this is the case.



15. A defibrillator is a device that gives an electric shock to a person whose heart has stopped beating normally.

DO NOT WRITE IN THIS MARGIN

This is shown in Figure 15A.



Two paddles are initially placed in contact with the patient's chest. A simplified defibrillator circuit is shown in Figure 15B.

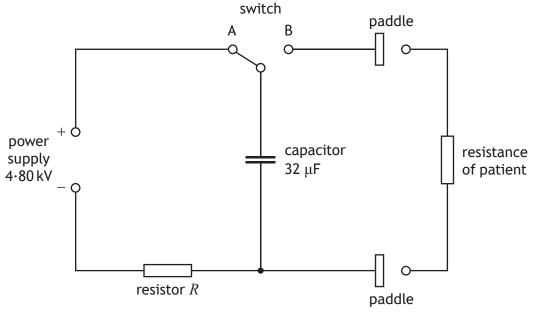


Figure 15B

When the switch is in position A, the capacitor is charged until there is a large potential difference across the capacitor.



15.	(cor	ntinued)	MARKS	DO NOT WRITE IN THIS MARGIN
	(a)	The capacitor can be considered to be fully charged after 5 time constants.		
		The time taken for the capacitor to be considered to be fully charged is 10.0s .		
		Determine the resistance of resistor <i>R</i> .	3	
		Space for working and answer		
	(b)	During a test, an 80.0 Ω resistor is used in place of the patient.		

The switch is moved to position B, and the capacitor discharges through the 80.0 Ω resistor.

The initial discharge current is 60 A.

The current in the resistor will fall to half of its initial value after 0.7 time constants.

Show that the current falls to 30 A in 1.8 ms.

Space for working and answer



15. (continued)

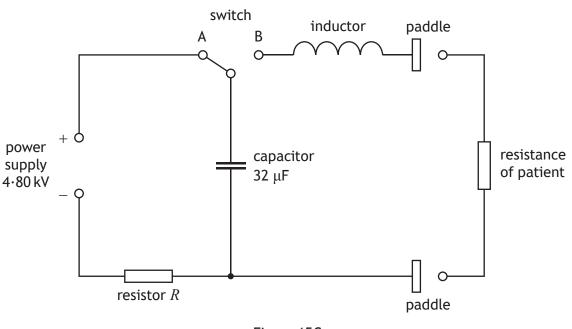
(c) In practice a current greater than 30 A is required for a minimum of $5 \cdot 0 \text{ ms}$ to force the heart of a patient to beat normally.

An inductor, of negligible resistance, is included in the circuit to increase the discharge time of the capacitor to a minimum of $5.0 \, \text{ms}$.

MARKS DO NOT WRITE IN

3

THIS



This is shown in Figure 15C.

Figure 15C

(i) The inductor has an inductance of 50.3 mH.

The capacitor is again fully charged. The switch is then moved to position B.

Calculate the rate of change of current at the instant the switch is moved to position B.

Space for working and answer



15. (c) (continued)

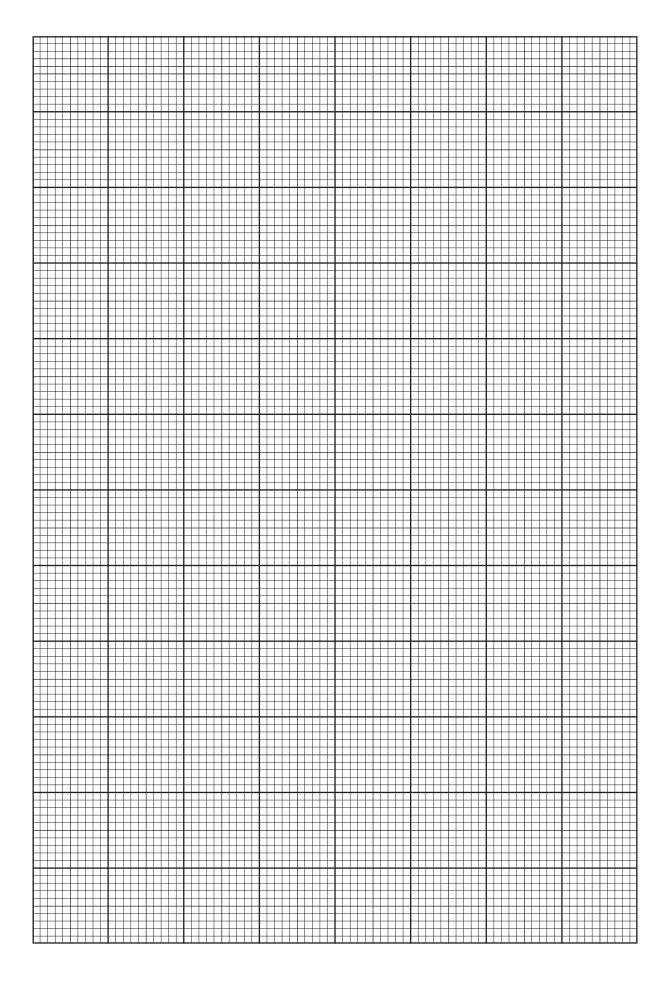
(ii) It would be possible to increase the discharge time of the capacitor with an additional resistor connected in the circuit in place of the inductor. However, the use of an additional resistor would mean that maximum energy was not delivered to the patient.

Explain why it is more effective to use an inductor, rather than an additional resistor, to ensure that maximum energy is delivered to the patient.

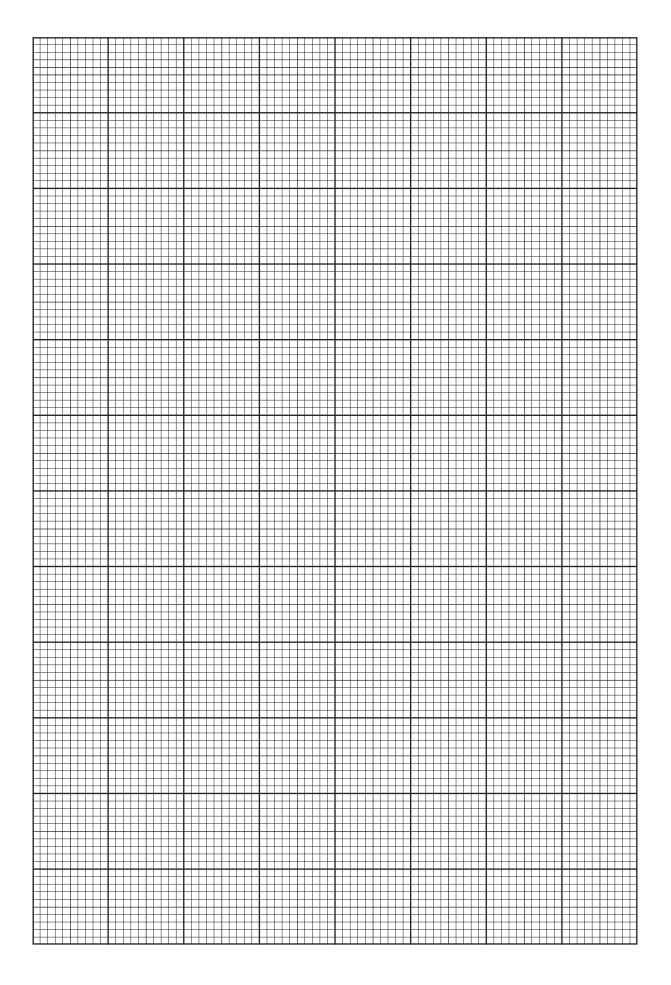
2

[END OF QUESTION PAPER]











ADDITIONAL SPACE FOR ANSWERS AND ROUGH WORK



ADDITIONAL SPACE FOR ANSWERS AND ROUGH WORK



ADDITIONAL SPACE FOR ANSWERS AND ROUGH WORK



[BLANK PAGE]

DO NOT WRITE ON THIS PAGE



ACKNOWLEDGEMENTS

Question 1 – Figure 1A – CG Stocker/Shutterstock.com

Question 3 – Figure 3A – dashadima/Shutterstock.com

Question 15 – Figure 15A – Luciano Cosmo/shutterstock.com





2018

X757/77/11

Physics **Relationships Sheet**

TUESDAY, 8 MAY 9:00 AM - 11:30 AM





$v = \frac{ds}{dt}$	$L = I\omega$
$a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$	$E_{K} = \frac{1}{2}I\omega^{2}$
v = u + at	$F = G \frac{Mm}{r^2}$
$s = ut + \frac{1}{2}at^2$	$V = -\frac{GM}{r}$
$v^2 = u^2 + 2as$	$v = \sqrt{\frac{2GM}{r}}$
$\omega = \frac{d\theta}{dt}$	apparent brightness, $b = \frac{L}{4\pi r^2}$
$\alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$	$4\pi r^2$ Power per unit area = σT^4
$\omega = \omega_o + \alpha t$	$L = 4\pi r^2 \sigma T^4$
$\theta = \omega_o t + \frac{1}{2}\alpha t^2$	$r_{Schwarzschild} = \frac{2GM}{c^2}$
$\omega^2 = \omega_o^2 + 2\alpha\theta$	E = hf
$s = r\theta$ $v = r\omega$	$\lambda = \frac{h}{p}$
$a_t = r\alpha$	$mvr = \frac{nh}{2\pi}$
$a_r = \frac{v^2}{r} = r\omega^2$	$\Delta x \Delta p_x \ge \frac{h}{4\pi}$
$F = \frac{mv^2}{r} = mr\omega^2$	$\Delta E \ \Delta t \ge \frac{h}{4\pi}$
T = Fr	4π F = qvB
$T = I\alpha$	$\omega = 2\pi f$
$L = mvr = mr^2\omega$	
	$\omega = \frac{2\pi}{T}$

$$a = \frac{d^2 y}{dt^2} = -\omega^2 y \qquad \qquad B = \frac{\mu_o I}{2\pi r}$$

$$y = A \cos \omega t \quad \text{or} \quad y = A \sin \omega t$$

$$v = \pm \omega \sqrt{(A^2 - y^2)}$$

$$E_{\kappa} = \frac{1}{2} m \omega^2 (A^2 - y^2)$$

$$E_{p} = \frac{1}{2} m \omega^2 y^2$$

$$y = A \sin 2\pi (ft - \frac{x}{\lambda})$$

$$E = kA^2$$

$$C = \frac{1}{\sqrt{\varepsilon_o \mu_o}}$$

$$t = RC$$

$$X_{c} = \frac{V}{I}$$

$$X_{c} = \frac{1}{2\pi fC}$$

$$E = -L \frac{dI}{dt}$$

$$\phi = \frac{2\pi x}{\lambda}$$

optical path difference = $m\lambda$ or $\left(m+\frac{1}{2}\right)\lambda$ where m = 0, 1, 2...

$$\Delta x = \frac{\lambda l}{2d}$$

$$d = \frac{\lambda}{4n}$$

$$\Delta x = \frac{\lambda D}{d}$$

$$n = \tan i_p$$

$$F = \frac{Q_1 Q_2}{4\pi \varepsilon_o r^2}$$

$$E = \frac{Q}{4\pi \varepsilon_o r^2}$$

$$V = \frac{Q}{4\pi \varepsilon_o r}$$

$$F = QE$$

$$V = Ed$$

$$F = IlB \sin \theta$$

$$E = \frac{1}{2}LI^{2}$$

$$X_{L} = \frac{V}{I}$$

$$X_{L} = 2\pi fL$$

$$\frac{\Delta W}{W} = \sqrt{\left(\frac{\Delta X}{X}\right)^{2} + \left(\frac{\Delta Y}{Y}\right)^{2} + \left(\frac{\Delta Z}{Z}\right)^{2}}$$

$$\Delta W = \sqrt{\Delta X^{2} + \Delta Y^{2} + \Delta Z^{2}}$$

$$\begin{array}{lll} d=\overline{vt} & W=QV & V_{peak}=\sqrt{2}V_{mv} \\ s=\overline{vt} & E=mc^2 & I_{peak}=\sqrt{2}I_{mv} \\ v=u+at & E=hf & Q=h \\ s=ut+\frac{1}{2}at^2 & E_x=hf-hf_0 & V=IR \\ v^2=u^2+2as & E_2-E_1=hf & P=IV=I^2R=\frac{V^2}{R} \\ s=\frac{1}{2}(u+v)t & I=\frac{1}{f} & R_T=R_1+R_2+\dots \\ W=mg & v=f\lambda & \frac{1}{R_T}=\frac{1}{R_1}+\frac{1}{R_2}+\dots \\ W=mg & v=f\lambda & R_T=R_1+R_2+\dots \\ W=mg & v=f\lambda & R_T=\frac{1}{R_T}=\frac{1}{R_T}+\frac{1}{R_T}+\frac{1}{R_T}+\frac{1}{R_T}+\dots \\ F=ma & S=\frac{\sin\theta_1}{\sin\theta_2} & V_1=\left(\frac{R_1}{R_1+R_2}\right)V_5 \\ E_y=Fd & n=\frac{\sin\theta_1}{\sin\theta_2} & V_1=\left(\frac{R_1}{R_1+R_2}\right)V_5 \\ E_x=\frac{1}{2}mv^2 & Sin\theta_c=\frac{1}{n} & C=\frac{Q}{V} \\ P=mv & I=\frac{k}{d^2} & C=\frac{Q}{V} \\ Ft=mv-mu & I=\frac{P}{A} & E=\frac{1}{2}QV=\frac{1}{2}CV^2=\frac{1}{2}\frac{Q^2}{C} \\ F=G\frac{Mm}{r^2} & path difference=m\lambda \text{ or } (m+\frac{1}{2})\lambda \text{ where } m=0,1,2\dots \\ t'=\frac{1}{\sqrt{1-(\gamma'_C)^2}} & random uncertainty=\frac{max, value-min, value}{number of values} \\ z=\frac{\lambda_{charrent}-\lambda_{cent}}{\lambda_{cost}} \\ z=\frac{v}{c} \end{array}$$

 $v = H_0 d$

Additional Relationships

Circle

circumference = $2\pi r$

area = πr^2

Sphere

area = $4\pi r^2$

volume = $\frac{4}{3}\pi r^3$

Trigonometry

 $\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$

 $\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$

 $\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$

 $\sin^2\theta + \cos^2\theta = \mathbf{1}$

Moment of inertia

point mass $I = mr^2$

rod about centre $I = \frac{1}{12}ml^2$

rod about end $I = \frac{1}{3}ml^2$

disc about centre
$$I = \frac{1}{2}mr^2$$

sphere about centre $I = \frac{2}{5}mr^2$

Table of standard derivatives

f(x)	f'(x)
sin ax	a cos ax
cos ax	$-a\sin ax$

Table of standard integrals

f(x)	$\int f(x)dx$
sin ax	$-\frac{1}{a}\cos ax + C$
cos ax	$\frac{1}{a}\sin ax + C$

		87 Fr 2,8,18,32, 18,8,1 Francium	55 Cs 2,8,18,18, 8,1 Caesium	37 Rb 2,8,18,8,1 Rubidium	19 K 2,8,8,1 Potassium	Lithium 11 Na 2,8,1 Sodium	1 Hydrogen 3 Li 2 1	Group 1 (1) H
	Lar	88 Ra 2,8,18,32, 18,8,2 Radium	56 Ba 3, 2,8,18,18, 8,2 Barium	38 Sr 1 2,8,18,8,2 Strontium	20 Ca 2,8,8,2 1 Calcium	Beryllium 12 Mg 2,8,2 Magnesium	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	Group 2
Actinides	Lanthanides	89 Ac 2,8,18,32, 18,9,2 Actinium	57 La 2,8,18,18, 9,2 Lanthanum	39 Y 2,8,18,9,2 Yttrium	21 Sc 2,8,9,2 Scandium	3)		
89 Ac 2,8,18,32, 18,9,2 Actinium	57 La 2,8,18, 18,9,2 Lanthanum	104 Rf 2,8,18,32, 32,10,2 Rutherfordium	72 Hf 2,8,18,32, 10,2 Hafnium	40 Zr 2,8,18, 10,2 Zirconium	22 Ti 2,8,10,2 Titanium	(4)		Key
90 Th 2,8,18,32, 18,10,2 Thorium	58 Ce 2,8,18, 20,8,2 Cerium	105 Db 2,8,18,32, 32,11,2 Dubnium	73 Ta 2,8,18, 32,11,2 Tantalum	41 Nb 2,8,18, 12,1 Niobium	23 V 2,8,11,2 Vanadium	5	Electr	Atc
91 Pa 2,8,18,32, 20,9,2 Protactinium	59 Pr 2,8,18,21, 8,2 Praseodymium	106 Sg 2,8,18,32, 32,12,2 Seaborgium	74 W 2,8,18,32, 12,2 Tungsten	42 Mo 2,8,18,13, 1 Molybdenum	24 Cr 2,8,13,1 Chromium	6	Symbol Electron arrangement Name	Electron Arr Atomic number
92 U 2,8,18,32, 21,9,2 Uranium	60 Nd 2,8,18,22, 8,2 Neodymium	107 Bh 2,8,18,32, 32,13,2 Bohrium	75 Re 2,8,18,32, 13,2 Rhenium	43 Tc 2,8,18,13, 2 1 Technetium	25 Mn 2,8,13,2 Manganese	Transitior	ement	Arrange r
93 Np 2,8,18,32, 22,9,2 Neptunium	61 Pm 2,8,18,23, 8,2 Promethium	108 Hs 2,8,18,32, 32,14,2 Hassium	76 Os 2,8,18,32, 14,2 Osmium	44 Ru 2,8,18,15, 1 Ruthenium	26 Fe 2,8,14,2 Iron	(7) (8)		Electron Arrangements of Elements omic number
94 Pu 2,8,18,32, 24,8,2 Plutonium	62 Sm 2,8,18,24, 8,2 Samarium	109 Mt 2,8,18,32, 32,15,2 Meitnerium	77 Ir 2,8,18,32, 15,2 Iridium	45 Rh 2,8,18,16, 1 Rhodium	27 Co 2,8,15,2 Cobalt	(9)		Elemen
95 Am 2,8,18,32, 25,8,2 Americium	63 Eu 2,8,18,25, 8,2 Europium		78 Pt 2,8,18,32, 17,1 Platinum	46 Pd 2,8,18, 18,0 Palladium	28 Ni 2,8,16,2 Nickel	(10)		τ. Σ
96 Cm 2,8,18,32, 25,9,2 Curium	64 Gd 2,8,18,25, 9,2 Gadolinium	111 Rg 2,8,18,32, 32,18,1 ¹ Roentgenium	79 Au 2,8,18, 32,18,1 Gold	47 Ag 2,8,18, 18,1 Silver	29 Cu 2,8,18,1 Copper	(11)		
97 Bk 2,8,18,32, 27,8,2 Berkelium	65 Tb 2,8,18,27, 8,2 Terbium	110 111 112 Ds Rg Cn 2,8,18,32, 2,8,18,32, 2,8,18,32, 32,17,1 32,18,1 32,18,1 Darmstadtium Roentgenium Copernicium	80 Hg 2,8,18, 32,18,2 Mercury	48 Cd 2,8,18, 18,2 Cadmium	30 Zn 2,8,18,2 Zinc	(12)		
98 Cf 2,8,18,32, 28,8,2 Californium	66 Dy 2,8,18,28, 8,2 Dysprosium		81 Tl 2,8,18, 32,18,3 Thallium	49 In 2,8,18, 18,3 Indium	31 Ga 2,8,18,3 Gallium	Boron 13 Aluminium	(13) 5 B	Group 3
99 Es 2,8,18,32, 29,8,2 Einsteinium	67 Ho 2,8,18,29, 8,2 Holmium		82 Pb 3, 2,8,18, 3, 32,18,4 m Lead	50 Sn 3, 2,8,18, 18,4 n Tin	32 Ge ,3 2,8,18,4 n Germanium	S N C	(14) 6 C	3 Group 4
100 Fm 2,8,18,32, 30,8,2 Fermium	68 Er 2,8,18,30, 8,2 Erbium		83 Bi 8, 2,8,18, ,4 32,18,5 Bismuth	51 Sb 2,8,18, 18,5 Antimony	33 AS ium Arsenic	Pho 2	(15) 7 X	4 Group 5
101 Md 2,8,18,32, 31,8,2 Mendelevium	69 Tm 2,8,18,31, 8,2 Thulium		84 Po ,5 ,5 32,18,6 th Polonium	52 Te 3, 2,8,18, 18,6 ny Tellurium	34 Se ,5 2,8,18,6 ic Selenium	S N 0	(16) 8 0	5 Group 6
102 No 2,8,18,32, 32,8,2 Nobelium	70 Yb 2,8,18,32, 8,2 Ytterbium		85 At 3, 2,8,18, 6 32,18,7 im Astatine	53 – 18,7 18,7 Induced	35 Br ,6 2,8,18,7 m Bromine	G N E	(17)	Group
103 Lr 2,8,18,32, 32,9,2 Lawrencium	71 Lu 2,8,18,32, 9,2 Lutetium		86 Rn 3, 2,8,18, 1,7 32,18,8 Radon	54 Xe 3, 2,8,18, 18,8 Xenon	36 Kr ,7 2,8,18,8 ^{1e} Krypton		2 Helium 10 2 8	7 Gro

[BLANK PAGE]

DO NOT WRITE ON THIS PAGE

[BLANK PAGE]

DO NOT WRITE ON THIS PAGE